

Discussion Paper Series – CRC TR 224

Discussion Paper No. 472 Project A 03

Why Don't Poor Families Move? A Spatial Equilibrium Analysis of Parental Decisions with Social Learning

Suzanne Bellue¹

November 2023

¹ CREST-ENSAE

Support by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) through CRC TR 224 is gratefully acknowledged.

Collaborative Research Center Transregio 224 - www.crctr224.de Rheinische Friedrich-Wilhelms-Universität Bonn - Universität Mannheim

Why Don't Poor Families Move? A Spatial Equilibrium Analysis of Parental Decisions with Social Learning^{*}

Suzanne Bellue[†]

October 18, 2023

Abstract

In the United States, less-educated parents tend to choose lower levels of parental inputs: they reside in bad neighborhoods and allocate little time to parent-child activities. I propose a spatial overlapping generation model of parental decisions about time and neighborhood quality with imperfect information and social learning. Specifically, young agents learn about the relevance of parental inputs through observing their neighbors. Crucially, however, they are prone to misinferences as they may not be able to perfectly correct for selection induced by income segregation. I calibrate the model using several United States representative datasets. The calibrated model matches targeted and non-targeted parental behavior moments across socioeconomic groups. I find a relatively modest level of parental delusion that increases inequality by 3% (income Gini index) and social immobility by 12% (intergenerational rank-rank). A housing voucher policy improves the neighborhood quality of eligible families, raising children's future earnings. When scaling up the policy, long-run and general equilibrium responses in parental beliefs amplify the policy effects. Inequality reduces, and intergenerational mobility improves.

Keywords: Neighborhood, Education, Human Capital, Learning, Social Mobility JEL classification: D13, D62, D83, E24, I2, J13, R2

[†]CREST-ENSAE

^{*}I am indebted to Michèle Tertilt for her continued and invaluable support and guidance in this project. In addition, I am very grateful to Klaus Adam, Giovanni Ballarin, Antoine Camous, Antonio Ciccone, Anne Hannusch, Georgi Kocharkov, David Koll, Tsung-Hsien Li, Giacomo Ponzetto, José Víctor Ríos Rull, Jan Sun, Minchul Yum and seminar and conference participants at the XXV Workshop on Dynamic Macroeconomics 2022 (Vigo), the Summer School in Urban Economics 2022, the SMYE 2022, the CRC retreat 2022, the ENTER Jamboree 2022, UCL, the University of Mannheim for helpful discussions and suggestions. I gratefully acknowledge financial support from the German Academic Exchange Service (DAAD) and the German Research Foundation (through the CRC-TR-224 project A03).

1 Introduction

In the United States, parental input choices differ between more- and less-educated parents. In particular, less-educated parents tend to allocate less time to active parent-child activities and reside in worse neighborhoods, two parental inputs that shape children's adulthood economic opportunities.¹ As less-educated parents tend to also work fewer hours under perfect information and rational expectations, the main explanations for these differences are less-educated parents having tighter budget constraints, higher attachment to low-quality neighborhoods, or being less effective at teaching their children.² However, are these explanations complete enough? Recently, Bergman et al. (2019) showed that loosening low-income parents' budget constraints through housing voucher programs alone does not lead to large increases in neighborhood quality, suggesting other mechanisms at play. In parallel, since Cunha et al. (2013), a growing strand of the empirical literature documents differences in beliefs about the relevance of parental inputs for children's development across socioeconomic groups, offering an additional explanation. Less-educated parents' underestimation of parental inputs' relevance could partly explain low parental input choices.

In this paper, I introduce social learning about the relevance of parental inputs into a quantitative spatial model of human capital accumulation and parental input decisions. Specifically, I depart from perfect information and assume agents are unaware of the relevance of parental inputs for adulthood human capital. They learn about it by observing people around them, their neighbors. Crucially, however, agents suffer selection neglect; they are prone to misinferences as they may not be able to perfectly correct for selection. Social learning—learning through interactions and observations of others—is a central learning channel (Frick et al., 2022), and selection neglect an experimentally documented cognitive bias (Enke, 2020).³ The proposed learning mechanism works as follows: suppose adulthood human capital depends on past parental inputs, parental human capital, and a random, idiosyncratic, and unobserved ability shock, which can be interpreted—to some extent as luck. Assume imperfect information about the parameter governing parental inputs' relevance for adulthood human capital. Agents must form beliefs about it before they make their parental decisions. Young adults have two sources of information to do so: their parent's

¹While the literature shows parental time is a prime factor influencing child skill formation (Heckman and Mosso, 2014), the difference in parental time between more- and less-educated parents is an established pattern in the United States and elsewhere (see Doepke et al. (2022) for a review). Neighborhoods' causal effect on children's development is studied by Chetty and Hendren (2018a) in the United States.

²See Guryan et al. (2008) for a discussion.

³This cognitive bias is called "assortativity neglect."

beliefs and the inference they make by observing their neighbors' current human capital and past parental inputs and background. Notice, however, that they do not observe their neighbors' ability shocks and may be unable to perfectly correct for the selection with respect to those unobservables. As a result, if relatively many low-ability-shock neighbors surround young adults, they might overestimate local ability shocks, leading to an underestimation of the relevance of parental inputs. Implicitly, they would attribute too much of the local average human capital to local ability shocks and too little to parental inputs. The reverse happens if relatively many high-ability-shock neighbors surround young adults.

The quantitative model uses an overlapping generation framework, where heterogenous parents choose two parental inputs: in which type of neighborhood to reside and how much time to allocate to their child's education. When making decisions, parents have formed beliefs about the relevance of parental inputs. They face budget and time constraints that depend on their current earnings, a function of accumulated human capital during childhood, and exogenously determined college education status. Perfectly competitive land developers provide housing in each neighborhood type. Consequently, income residential segregation results from parents' residential decisions and local rents, which are equilibrium objects. Since ability shocks affect adulthood earnings, income residential segregation is a form of spatial sorting partly based on those shocks. In low-quality neighborhoods, with low equilibrium rent prices, relatively many low-ability-shock adults—who tend to be poorer—surround young adults. Conversely, in high-quality neighborhoods, relatively many high-ability-shock adults surround young adults. As a result, with social learning and selection neglect, young adults raised in low-quality neighborhoods might tend to underestimate the relevance of parental inputs for human capital. In contrast, young adults raised in high-quality neighborhoods might tend to overestimate it. In equilibrium, if there is selection neglect, income segregation generates information friction, leading to systematic misinferences across socioeconomic groups and persistence in beliefs within families. Children of low-belief and low-income parents are likely to live in low-quality neighborhoods, become poor parents next period, and underestimate the relevance of parental inputs. The reverse happens to children of high-belief and high-income parents.

This model embeds the main explanations for the socioeconomic differences in parental input choices: the child skill technology implies differences in returns to parental inputs by parental human capital—capturing differences in teaching effectiveness,—agents have a preference for their childhood neighborhood—capturing attachment for a given type of neighborhood which can be viewed as a moving cost,—and differ in their education status and earnings that determine their labor supply and budget constraints. In addition, parents have endogenously formed beliefs about the relevance of parental inputs for adulthood human capital. Given the model structure and the social learning process, there are multiple critical equilibrium objects: the distribution of human capital, parental beliefs, neighborhood choices, and local rents, which are endogenously determined as fixed points.

The model is solved numerically and calibrated to match a set of critical moments from several United States representative datasets. The model comprises ten neighborhoods, quality-ranked and matches segregation, and family earnings dispersion in the average commuting zone in the United States computed from the ACS 2000 and NHGIS 2000 datasets.⁴ In addition, it targets causal neighborhood effects on children's future incomes estimated by Chetty and Hendren (2018b) and social mobility measured by Chetty et al. (2014). Parents' decisions are disciplined by matching active parental time in the ATUS survey and neighborhood quality choices from AddHealth. Even though the model does not feature preference heterogeneity, the calibrated model matches parental behavior across socioeconomic groups well: it provides a rationale for college parents allocating more time to their children's education than non-college parents despite working more hours and correctly matches non-targeted intergenerational residential mobility patterns.

In contrast, a perfect information version of the model cannot replicate the data without imposing sizable heterogeneous preferences across childhood neighborhoods and education status. To see this, I first re-calibrate the model, shutting down selection neglect and, consequently, the parental beliefs channel. Unsurprisingly, the alternative calibrated model misses all the non-targeted parental behavior moments. I then introduce quadratic moving costs, and education-specific altruism parameters and define the same targeted moments as in the baseline model. This extended alternative version of the model misses the parental time gradient in earnings and untargeted residential mobility moments. To improve the model fit regarding residential mobility, agents born in bottom-quality neighborhoods must like their childhood neighborhood type thirty times more than the others. This necessary feature is at odds with the empirical findings of Bergman et al. (2019) who compare lowincome families who live in deprived neighborhoods and are randomly allocated between treatment and control groups. They find that parents in the treatment group, induced to move to higher-quality neighborhoods, are more satisfied and willing to stay in their new neighborhood than those in the control group.

 $^{^{4}}$ I proxy neighborhood "quality" with neighborhoods' median household income that correlates with places' effects measured by Chetty and Hendren (2018b) but also with low poverty, crime, and high-performing schools.

Using the calibrated baseline model, I first find that parental beliefs explain a large share of the socioeconomic gap in parental input choices. In particular, providing full information about the relevance of parental inputs would improve low-income parents' beliefs by 17% and decrease those of high-income parents by 7%. Those numbers are of a reasonable order of magnitude compared to empirical estimates.⁵ Importantly, parental beliefs have sizable effects on the economy. Children born in bottom-quality neighborhoods would be half as likely to remain in those neighborhood types in adulthood, and low-income parents would allocate 31% more time to their children's education. Perfect information about the relevance of parental inputs would decrease the rank-rank slope, a measure of social immobility, by 12%, and the Gini index of income, a measure of inequality, by 3%, improving welfare by 0.6%.

The model features two key frictions that motivate a policy intervention. Parents cannot borrow against their children's future earnings, and due to social learning and selection neglect, income residential segregation generates information frictions that distort parental decisions. Motivated by the evidence that housing vouchers improve the neighborhood quality of eligible families (Chetty et al., 2016), I use the calibrated model to study their effects on the United States economy. I consider a housing voucher covering the difference between 30% of income and the rent up to a limit. Eligible households are parents from the bottom decile of the income distribution. In the first step, I study the partial equilibrium effects of the policy by simulating a randomized control trial within the model. Compared to the control group—eligible parents who do not receive housing vouchers,—eligible parents who receive the vouchers live in higher-quality neighborhoods, positively affecting their children's earnings at age 26 by \$663 a year.⁶ Beliefs play a substantial role. If parents had perfect information about the relevance of neighborhood quality for their child's future earnings, they would move to 0.4 higher-rank-quality neighborhoods, increasing their children's earnings by an additional \$132 per year.

The second main finding is that, when scaling up the housing voucher policy, general equilibrium responses in local prices and, in particular, in beliefs amplify the partial equilibrium effects. The voucher allows housing voucher holders to move to better neighborhoods, increasing the density in middle-range quality neighborhoods—especially at the rent limit—and forcing non-eligible households to move out. The housing market reaction creates

⁵Cunha et al. (2013) elicit maternal expectations about the technology of skill formation from a sample of socioeconomically disadvantaged African American women. The author's favorite estimates of the percentage difference between the actual and the believed returns to investment range between 4 and 39%.

⁶The effects on children's earnings enter the confidence interval of the empirical estimates from Chetty et al. (2016).

winners and losers, with adverse effects in the aggregates; however, in the long run, information and parental beliefs improve, particularly among low-income households, amplifying partial equilibrium effects on eligible families and generating positive effects on measures of intergenerational mobility (+3.8%), and equality (+0.8%).

Despite positive long-run effects, a housing voucher policy with a unique rent limit at the commuting zone has unintended consequences. It generates a bunching behavior of eligible households at the rent limit in middle-range quality neighborhoods. The housing market remains highly segregated, and high-income families continue having too-high parental beliefs. Designing a housing voucher policy with rent limits set at a more granular level is a better tool for mitigating the distorting effects of parents' beliefs. Under an alternative housing voucher policy with multiple rent limits, in the long run, intergenerational mobility improves by 8.5%, and inequality decreases by 1.5%.

Related Literature

This paper links several strands of the literature: the education literature and the beliefs literature, the quantitative family-macroeconomics literature, and the quantitative spatial economics literature.

First, this paper builds on empirical evidence from the parental beliefs literature. Since Cunha et al. (2013), a large body of research documents that actual technology of skill formation does not systematically differ by socioeconomic groups but that parents' beliefs about the technology of skill formation differ, correlate with income and influence their decisions (see for instance Jensen (2010); Attanasio and Kaufmann (2014); Kaufmann (2014); Caucutt et al. (2017); Boneva and Rauh (2016, 2018); Belfield et al. (2019); Dizon-Ross (2019); Wiswall and Zafar (2021)).⁷ A central channel through which people learn about their societies is through social learning—by observing the history and outcomes among their peers (Frick et al., 2022),—and the behavioral and psychological literature documents selection neglect (Enke, 2020).⁸ Relatedly, the empirical education literature highlights the importance of role models, and, in some cases, to the selection in the observation of those role models. For instance, low-income children lacking successful role models among their peers could explain the low levels of motivation and effort (Nguyen, 2008; Alan et al., 2019; Breda

⁷One exception is Attanasio et al. (2019) in the UK who does not find a socioeconomic gradient in beliefs. ⁸The literature provides evidence of social learning with selection neglect in different settings. An empirical example of the role of social learning and selection neglect for technology adoption is given by Conley and Udry (2010). In rural Ghana, the authors find that the use of fertilizer by small farmers is boosted by the observation of surprisingly successful peer farmers.

et al., 2019; Algan et al., 2020; Guyon and Huillery, 2020). Recently, Chetty et al. (2022) find that the share of high socioeconomic status friends in a ZIP code best predicts upward income mobility in the United States and propose social learning as one likely explanation for it. In the model, I develop a social learning process with selection neglect and extend it to learning about the child's skill technology.

Second, this paper quantifies the macroeconomic effects of endogenous beliefs by incorporating social learning into a quantitative spatial model of overlapping generations in which parents affect their child's human capital by choosing their neighborhood and parental time. By doing so, I contribute to the quantitative family macroeconomics literature. Human capital accumulation is modeled following recent macroeconomic papers such as Daruich (2018); Jang and Yum (2020); Kim et al. (2021); Yum (2022); Chyn and Daruich (2022). While in other sub-areas of macroeconomics, such as finance, individuals' beliefs are considered critical elements in explaining agents' investment behavior (see, for instance, Adam et al. (2017)), heterogeneous beliefs are usually ignored in family macroeconomics. Two major exceptions are Fogli and Veldkamp (2011) and Fernández (2013) who rationalize the change in female labor supply over time by a change in beliefs. In this paper, the learning process builds on Fogli and Veldkamp (2011). A key difference is the introduction of residential choices, which, combined with a selection neglect modeled as in Bénabou and Tirole (2005), generates a bias. In equilibrium, the learning process generates a stable distribution of heterogeneous parental beliefs that affect parental input choices. While the idea of neighborhood effects through social learning has been largely developed (see, for instance, Durlauf (2011)), very few papers have linked heterogeneous beliefs with residential choices. Roemer and Wets (1994); Streufert (2000) are two exceptions. They provide different theoretical frameworks in which the selection induced by residential sorting could lead to systematic bias in beliefs. However, this paper is the first to develop and calibrate a quantitative model with social learning and residential choices.

Finally, the paper contributes to the neighborhood literature by linking segregation and inequality. I use methods from the quantitative spatial economics literature reviewed in Redding and Rossi-Hansberg (2017). Motivated by recent evidence of a causal relationship between exogenous neighborhoods and child's skills (Chyn, 2018; Chetty and Hendren, 2018a,b; Hwang, 2022; Nakamura et al., 2022), the model displays exogenous amenities. As in Fogli and Guerrieri (2019); Eckert et al. (2019); Chyn and Daruich (2022); Gregory et al. (2022), neighborhoods' environment quality directly affects children's future human capital. By having endogenous valuations of neighborhood quality through beliefs, I contribute to the growing literature that considers endogenous neighborhood amenities (Ahlfeldt et al., 2015; Diamond, 2016; Bilal, 2021). A few papers have quantitatively linked segregation and inequality. Fogli and Guerrieri (2019) and Gregory et al. (2022) incorporate peer effects in spatial equilibrium, and Eckert et al. (2019); Chyn and Daruich (2022) model the effect of local taxes on neighborhood environment quality. This model provides and quantifies a new mechanism for the relationship between segregation and inequality. Segregation creates informational frictions: the more the economy is segregated, the steeper the socioeconomic gradient in parental beliefs and, consequently, parental input choices.

The remainder of the paper proceeds as follows. Section 2 presents the spatial overlapping generations model. Section 3 explains the model calibration and presents some quantitative results. Section 4 uses the model for policy analysis, and Section 5 concludes.

2 The Model

Consider one labor market composed of a finite number of neighborhoods populated by families of one parent and one child. Children's future earnings depend on childhood neighborhood quality, parental time, parental human capital, and an unobserved idiosyncratic ability shock. Parents decide on two parental inputs of the child skill technology: in which neighborhood to raise their child and how much time to spend on their child's education. Sorting across neighborhoods within the labor market is only driven by families seeking better opportunities for their children. One of the key features of the model is imperfect information and social learning about the returns to parental inputs. Before making decisions, young agents learn about the returns using the information available at the neighborhood level.

The following sections describe the economic environment, the novel mechanism—social learning within neighborhoods—the parents' optimization problem, and the housing market. Then I give the equilibrium definition.

2.1 Economic Environment

Geography and Amenities: Consider one commuting zone with a finite number of ex-ante heterogeneous neighborhoods. Neighborhoods differ in quality m. Thus, a neighborhood is characterized by its quality m rather than its particular name. As wages do not vary across neighborhoods, neighborhood quality is the only exogenous amenity.

Families: The economy is populated by a continuum of families composed of one parent and one child. Time is discrete and each agent lives for two periods: childhood and parenthood. Parents choose in which neighborhood to raise their child and on how much time to spend on their child's education—parental time. Families are heterogeneous concerning four parental characteristics: accumulated human capital, college graduation status, the neighborhood of birth, and subjective beliefs about the technology of skill formation.

In the following, primed letters correspond to children's next period variable, lowercase letters to parents' variables, and uppercase letters to grand-parents' variables.

Technology of Skill Formation: Children's next period human capital h' mainly depends on their parent as it is a function of their childhood neighborhood quality m, parental time τ , parental human capital h, and ability shock a'. The functional form is as follows:

$$h' = (i(m, \tau) + \underline{i})^{\alpha} h^{\beta} \exp(a')$$

$$i(m, \tau) = \left(\gamma \left(\frac{\tau}{\overline{\tau}}\right)^{\varphi} + (1 - \gamma) m^{\varphi}\right)^{\frac{1}{\varphi}},$$

(1)

where α , β , $\gamma \in (0,1)$ and the child's ability shock a' is uncorrelated with parental characteristics and drawn from a normal distribution $\mathcal{N}(0, \sigma_a)$.⁹ Crucially, ability shocks are imperfectly observed.

By assumption, parental human capital h enhances the productivity of the two parental inputs. This feature seeks to capture that high-human capital parents are better at building child skills and that environmental factors, such as in-utero experiences correlated with parental human capital, influence children's skills (Cunha and Heckman (2007, 2009); Cunha et al. (2010); Heckman and Mosso (2014)). Following the literature, I assume a nested CES function for the skill formation technology, with one of the elasticities set to unity which imposes a parsimonious Cobb-Douglas outer form.¹⁰ Following Kim et al. (2021), the parameter $\underline{i} > 0$ guarantees that every child has a minimal level of baseline human capital. This term captures, for instance, a uniform minimum level of public education across neighborhoods. Finally, parental τ is normalized by its baseline unconditional mean

⁹By assuming uncorrelated ability shocks across generations, I abstract from modeling genetics. If one added it, incentives to invest would be distorted as high human capital parents would already expect their child to have high ability shocks. However, the main results of the paper would go through. In particular, the relative importance of h in the technology of skill formation captures part of a genetic effect.

¹⁰For similar modeling assumptions, see for instance Fuchs-Schündeln et al. (2022); Jang and Yum (2020); Lee and Seshadri (2019); Yum (2022).

 $(\overline{\tau})$ to achieve unit independence and computational stability following Jang and Yum (2020).

College Graduation Probability: To connect the model outputs to the data, I introduce college graduation status. Each child has a positive probability of entering and graduating from college. The college graduation probability g(h', h, s) depends on the parent's schooling status, earnings, and the child's accumulated human capital. Agent's schooling status s is equal to one if the agent graduated from college, zero otherwise.

Parents' Earnings: Parents' earnings are a function of accumulated human capital h, college graduation status s and exogenous working time $\overline{\ell_s} > 0$. Exogenous working time depends on the college graduation status s and embeds differences in working hours resulting from non-modeled labor market frictions. Parents' earnings are:

$$y = w \ h \ (1 + \omega s) \ \overline{\ell_s},$$

with w the rental rate of human capital, which is exogenous and common across households and neighborhoods. The college premium is captured by ω .

Parents' Preferences: Parents consume and enjoy leisure. In addition, they are altruistic as their child's value enters their utility function. Preferences of a parent raised in childhood neighborhood quality m_0 , and with subjective beliefs $\tilde{\alpha}$ can be summarized by the following utility function:

$$\log\left(c\right) + \frac{\left(1 - \overline{\ell_s} - \kappa \tau\right)^{1 - \frac{1}{\psi}}}{1 - \frac{1}{\psi}} + \iota \mathbb{1}_{m_0 = m} + \nu \varepsilon_m + b \mathbb{E}\left[\mathcal{V}\left(h', s', m, \tilde{\alpha}\right) | \tilde{\alpha}\right],$$

where b is a strength of altruism. Parents derive utility from consumption c and enjoy leisure, defined as one unit of time minus working time and parental time: $1 - \overline{\ell_s} - \kappa \tau$. Parental time τ is weighted by κ , showing that parents might value time spent at work differently than with their child. The curvature of the utility function with respect to leisure is $-\frac{1}{\psi}$. Parents have a preference for their childhood neighborhood quality that is captured by ι . In addition, parents have an idiosyncratic taste shock over neighborhoods ε_m . This shock captures moving motives that are uncorrelated with the neighborhood quality. I assume this shock is i.i.d. across neighborhood qualities and over time and distributed according to a Type-I Extreme Value with parameters $(-\bar{\gamma}, 1)$, where $\bar{\gamma}$ is the Euler-Mascheroni constant which ensures that the distribution has zero mean. The dispersion of the idiosyncratic neighborhood taste shock is measured by ν . Finally, $\tilde{\alpha}$ stands for the parent's subjective beliefs regarding the value of parameter α in the technology of skill formation and E [$\mathcal{V}(h', s', m, \tilde{\alpha})$ | $\tilde{\alpha}$] is the expected child lifetime utility with respect to the child's ability shock and neighborhood taste shock conditional on the parent's subjective beliefs $\tilde{\alpha}$.

Housing Supply: There are perfectly competitive land developers who produce housing on a unit endowment of land in each neighborhood with an isoelastic production function: $\mathcal{H}_m = \zeta r_m^{\eta}$, where ζ and η are parameters, with η the price elasticity of housing supply. Equilibrium rents per housing unit $\{r_m\}$ are determined by rental market clearing, such that housing demand equals housing supply in each neighborhood.

Aggregate Rent Rebates: Rents are redistributed to all families with a non-distortionary flat earnings subsidy. Every household receives a rebate from aggregate rent payments equal to R, where R is the economy's average rent payments.

2.2 Social Learning

One key and novel feature of the model is the social learning process. Following Fogli and Veldkamp (2011), learning happens in the first period of life, before parental decisions, using two sources of information: inherited parent's beliefs ($\tilde{\alpha}$) and own inference through the observation of outcomes and history in neighborhood m ($\hat{\alpha}_m$).

The inference process of $\hat{\alpha}_m$ requires several assumptions, regarding (i) agents' knowledge of the economy, (ii) the set of information agents have access to, (iii) the cognitive bias they suffer from, and (iv) the way they infer the unknown parameter α .

First, young agents know everything about the model but α , the elasticity of adulthood human capital with respect to the combination of parental inputs. They know the functional form of the technology of skill formation—but α ,—the randomness of the ability shock and the parent's problem. The mental model in log form young agents use for an adult j in a given neighborhood m is then:

$$\log h_i = \alpha \, \log \left(i(M_i, \, \mathbf{T}_i) \, + \, \underline{i} \right) \, + \, \beta \, \log H_i \, + \, a_i, \quad j \in m,$$

where T_j and M_j represent past parental choices, and H_j represents past parental human capital in family j.

Second, young agents' information set is restricted to their neighborhood. They only observe their neighbors, and, more specifically, local aggregates. Assuming agents would know all their neighbors' outcomes would be unrealistic, but by talking to neighbors and reading local news, I assume they have a good sense of local averages. Crucially, however, young agents do not observe ability shocks, which prevent them from immediately inferring the value of α .

Third, I depart from rational expectations and introduce a cognitive bias, namely selection neglect. Even though agents know the parents' problem, they might not fully understand the spatial sorting process in the economy and may not be able to perfectly infer local ability shocks. In a given neighborhood m, young agents' perceived average local ability shock is given by:

$$\overline{\tilde{a}}_m = \overline{a}_m + \pi(\overline{a} - \overline{a}_m),$$

where $\overline{\tilde{a}}_m$ represents perceived average ability shock in neighborhood m, \overline{a}_m the actual average ability shock in neighborhood m and \overline{a} the average ability shock in the economy. Following Bénabou and Tirole (2005)'s modeling, the strength of the cognitive bias is governed by $\pi \in [0, 1]$. With $\pi = 0$ implying young agents are perfectly able to infer local ability shocks, i.e., there is no selection neglect and $\pi = 1$ young agents mistakenly think of their neighbors as a representative sample of the population, i.e., there is full selection neglect.¹¹ The following equation describes the observations and perceptions of every young agent in a given neighborhood m:

$$\overline{\log h}_m = \alpha \ \overline{\log \left(i(M, \ \mathbf{T}) \ + \ \underline{i}\right)}_m \ + \beta \ \overline{\log H}_m \ + \ \overline{\tilde{a}}_m,$$

where $\overline{\log(i(M, T) + \underline{i})}_m$ stands for the local average in the combination of pas parental inputs, and $\overline{\log h}_m, \overline{\log H}_m$ current and past average human capital in neighborhood m.

Finally, every young agent uses her observation of local averages to infer the relevance of parental inputs governed by α :¹²

$$\hat{\alpha}_m = \frac{\overline{\log(h)}_m - \beta \overline{\log H}_m - \overline{\tilde{a}}_m}{\overline{\log(i(\mathbf{T}, M) + \underline{i})}_m}$$

Notice that young agents' inference of the relevance of parental inputs $(\hat{\alpha}_m)$ is downward biased if local ability shocks are relatively low and agents overestimate them $(\overline{\tilde{a}}_m \geq \overline{a}_m)$ and upward biased if local ability shocks are relatively high and agents underestimate them $(\overline{\tilde{a}}_m \leq \overline{a}_m)$. Intuitively, when young agents overestimate ability shocks, they implicitly

¹¹One way to micro-found the bias strength π is through unbiased but bounded signals about ability shocks, as in Jehiel (2018). See Appendix C for more details. Notice that if young agents were to observe everyone in the economy or without residential sorting, then $\bar{a} = \bar{a}_m$, which makes the selection neglect bias irrelevant. In that case, and similar to Fogli and Veldkamp (2011), there would be convergence in beliefs toward the truth.

¹²An alternative would be that agents observe individual outcomes of a given number of neighbors and run an OLS regression. To make this assumption realistic, one would have to draw, randomly or not, the number of neighbors each agent observes. This deviation would make the model richer but wouldn't change the paper's main intuitions.

attribute too much of the local human capital to ability shocks and too little to past parental inputs, underestimating the elasticity of human capital with respect to the combination of parental inputs.

Once they have inferred the value of α with local observations, young agents then update their inherited subjective beliefs using a weighted average of both:

$$\tilde{\alpha}' = \mu \hat{\alpha}_m + (1 - \mu) \tilde{\alpha},\tag{2}$$

with $\mu \in (0, 1)$ capturing the weight young agents put on their own experience versus parental beliefs and telling.

2.3 Parents' Problem

Parents are the only decision-makers in the economy. They make three decisions, of which two affect their child's next period human capital: neighborhood quality m and parental time τ . The timing is as follows: parents observe their idiosyncratic taste shocks for neighborhoods, take rents as given, and make decisions by maximizing their utility conditional on their subjective belief about the returns to parental inputs ($\tilde{\alpha}$). The maximization problem is the following:

$$\mathcal{V}(h, s, m_0, \tilde{\alpha}) = \max_{c, \tau, m} \{ \log (c) + \frac{\left(1 - \overline{\ell_s} - \kappa \tau\right)^{1 - \frac{1}{\psi}}}{1 - \frac{1}{\psi}} + \iota \mathbb{1}_{m_0 = m} + \nu \varepsilon_m + b \mathbb{E} \left[\mathcal{V}(h', s', m, \tilde{\alpha}) | \tilde{\alpha} \right] \}$$
(3)

subject to:

$$c + r_m = w h (1 + \omega s) \ell_s + R$$

$$\tau \in [0, 1 - \overline{\ell_s}]$$

$$h' = f(\tau, m, h, a' | \tilde{\alpha}), \quad a' \sim \mathcal{N}(0, \sigma_a)$$

$$p(s' = 1) = g(h', h, s),$$

where r_m is the equilibrium rent of neighborhood m, $E[\mathcal{V}(h', s', m, \tilde{\alpha}) | \tilde{\alpha}]$ is the expected child's utility conditional on the ability and the neighborhood taste shocks, and f(.) is the technology of skill formation defined by (1). Parents decide how to allocate their income into consumption c and housing costs r_m , and one unit of time into leisure, exogenous working hours, and parental time.

2.4 Housing Market

Let $U = E(\mathcal{V})$ denote the expected lifetime utility of a representative parent with respect to the vector of idiosyncratic neighborhood taste shocks ε_m . Let $V(h, s, m_0, \tilde{\alpha}, m | r_m) =$ $\log(c_m^*) + \frac{(1-\overline{\ell_s}-\kappa \tau_m^*)}{1-\frac{1}{\psi}}^{1-\frac{1}{\psi}} + \iota \mathbb{1}_{m_0=m} + b \mathbb{E}[\mathcal{V}(h', s', m, \tilde{\alpha}) | \tilde{\alpha}]$ the utility derived from living in neighborhood m abstracting from the neighborhood taste shock, with c_m^* and τ_m^* the optimal parent's choices given the neighborhood m and the rent price r_m .

Under the Type-I Extreme Value assumption, the expected lifetime utility of a parent is:

$$U(h, s, m_0, \tilde{\alpha}) = \nu \log \sum_m \exp\{\frac{1}{\nu} V(h, s, m_0, \tilde{\alpha}, m | r_m)\}.$$

The share of parents who choose to locate in neighborhood quality m among parents with human capital h, graduation status s, raised in neighborhood quality m_0 and with subjective beliefs $\tilde{\alpha}$ is :

$$\lambda_m(h, s, m_0, \tilde{\alpha} | r_m) = \frac{\exp\{\frac{1}{\nu} V(h, s, m_0, \tilde{\alpha}, m | r_m)\}}{\sum_n \exp\{\frac{1}{\nu} V(h, s, m_0, \tilde{\alpha}, n | r_n)\}}.$$

In equilibrium, rent prices are such that housing demand equals housing supply in each neighborhood m:

$$\sum_{m_0} \sum_{s} \int \int \lambda_m(h, s, m_0, \tilde{\alpha} | r_m) F(h, s, m_0, \tilde{\alpha}) \, dh \, d\tilde{\alpha} = \zeta r_m^{\eta}, \tag{4}$$

with $F(h, s, m_0, \tilde{\alpha})$ the joint distribution of human capital, graduation status, neighborhood of birth, and subjective beliefs

2.5 Equilibrium

The key objects of the equilibrium in the steady state are the endogenous distribution of human capital, subjective beliefs, and rent prices. For a given initial human capital, graduation status, neighborhood of birth, and subjective belief distribution $F_0(h, s, m_0, \tilde{\alpha})$, an equilibrium is characterized by a sequence of residential and parental time choices, $\{m\}$ and $\{\tau\}$, a sequence of rents $\{r_m\}$ for each neighborhood, and a sequence of distributions $\{F(h, s, m_0, \tilde{\alpha})\}$, such that the following four conditions are satisfied:

- 1. agents solve (3).
- 2. housing market clearing: rent prices $\{r_m\}$ ensure housing demand equals supply in every neighborhood according to (4).
- 3. beliefs update: young agents update their inherited beliefs according to (2).
- 4. earnings, graduation status, place of birth, and subjective beliefs consistency: those are consistent with the parent's income, graduation status, subjective beliefs, and decisions.

Details on how I compute the steady state equilibrium are provided in Appendix B.

3 Calibration

I numerically solve the model as detailed in Appendix B and calibrate it to the average United States commuting zone in the 2000s. The calibration proceeds in multiple steps. First, some parameter values are directly estimated from the data. Second, others are chosen externally based on direct data analogs, the literature, or simple normalization, and finally, the remaining parameters are selected to match relevant data moments. To validate the model, I then compare the model's predictions to non-targeted moments.

3.1 Preliminaries

I let the discrete distribution for *a* to approximate a normal distribution $a \sim \mathcal{N}(0, \sigma_a)$ which I discretize using Tauchen (1986), with a ten-point grid. Finally, I assume the technology of skill formation has constant returns to scale, $\beta = 1 - \alpha$.

I use multiple data sources to compute the relevant moments to calibrate the model. Earnings distribution moments come from the American Community Surveys (ACS) from 2000. I use the information at the census tract level from the National Historical Geographic Information System (NHGIS) dataset in 2000 (Manson et al., 2022) to construct neighborhood sociodemographic characteristics. I aggregate census tract information at the commuting zone level using a county-to-commuting zone crosswalk. Neighborhood choices and college graduation probabilities are estimated using data from the AddHealth survey described in Appendix Section A.1.¹³ Finally, parents' time use information is taken from the American Time Use Survey (ATUS) 2003.¹⁴

¹³See Appendix Section D.3 for more details on those statistics.

¹⁴Appendix Section A.3 provides detailed information on how I compute parental time using ATUS.

3.1.1 Geography

The model is calibrated to the average commuting zone in the United States, matching neighborhoods' impact estimated by Chetty and Hendren (2018a) in the 100 biggest commuting zones. To be consistent, I only use the top 100 commuting zones in NHGIS 2000. I set the number of neighborhoods in the model to ten, representing a synthetic decile census tract in the data. Specifically, in each of the 100 commuting zones of the NHGIS 2000, I sort census tracts by median household income and form ten synthetic neighborhoods from the deciles of this distribution.¹⁵ I then create one average commuting zone by computing the population-weighted average characteristics of each of the ten neighborhoods.¹⁶

3.2 Empirically Estimated Parameters

Housing Markets: Rental prices are determined in equilibrium given the supply function: $\mathcal{H}_m = \zeta r_m^{\eta}$, where r_m is the equilibrium rent price in the neighborhood m, and η is the price elasticity of housing supply. η and ζ can be estimated directly from the synthetic neighborhood density and rents.^{17,18}

College graduation probability: The college graduation probability depends on the parent's education and earnings and the child's accumulated human capital. Following Blandin and Herrington (2022) and using AddHealth, I estimate the following weighted logit regression of college completion:

$$g(h', y, s) = \frac{1}{1 + \exp(-(\gamma_1 + \gamma_2 rank_{h'} + \gamma_3 rank_y + \gamma_4 s))},$$

where g(h', y, s) is the binary outcome of either graduating college or not in Wave V, s = 1 if the highest level of education of the mother is above or equal to a bachelor's degree, $rank_{h'} \in \{1, 2, ..., 10\}$ is the human capital rank proxied by the grade rank in Wave II of the interviewed adolescent in 1996, and $rank_y \in \{1, 2, ..., 10\}$ is the household income rank in

¹⁵I use median household income as a proxy for neighborhood quality because it is one of the variables that correlates the most with place-based effects within commuting zones of Chetty and Hendren (2018a). Using their estimates, I find that growing up in one standard deviation higher median income county within a commuting zone increases a given child's income by 1.9%.

¹⁶Appendix Table S3 summarizes the ten neighborhoods' characteristics.

 $^{^{17}}$ Appendix Figure S2 summarizes the log-relationship between density (Column (5) Table S3) and rents across the ten synthetic neighborhoods.

¹⁸Note that in the literature, ζ is sometimes neighborhood specific (ζ_m). In this context, density and rent prices have an almost linear log relationship (see Appendix Figure S2); I choose to have the same ζ value across neighborhoods. Without loss of generality, the numeraire is the average household earnings in the economy.

3.3 Externally Calibrated Parameters

The parameter $\frac{1}{\psi}$ governs the curvature of the utility function with respect to leisure. I set the intertemporal elasticity of substitution ψ to 0.5, as is standard in the literature. I assume agents have an endowment of one unit of time corresponding to sixteen hours per day in the data.²⁰ The fraction of time allocated to market work by education comes from ATUS 2003, as described in Appendix Section A.3. The wage rate w, the parental investment constant \underline{i} , and the average neighborhood quality is normalized to 1. I assume the number of neighborhoods N is equal to ten, and neighborhood quality is distributed according to $m \sim U(\underline{m}, \overline{m})$. Table 1 summarizes the externally calibrated parameters.

Parameter Description		Value	Source			
N	Number of neighborhoods	10	Deciles NHGIS			
β	Returns on parental human capital	$1 - \alpha$	Constant returns			
$\frac{\frac{\beta}{\ell_0}}{\frac{\ell_1}{\ell_1}}$	Non-college labor supply	0.275	ATUS 2003			
$\overline{\ell_1}$	College labor supply	0.294	ATUS 2003			
ψ	Intertemporal elasticity of substitution	0.5	Standard			
w	Wage rate	1	Normalization			
i	Parental investment constant	1	Normalization			
μ_m	Average neighborhood quality	1	Normalization			
ζ	Housing supply coefficient	-1.04	NHGIS			
η	Price elasticity of housing supply	0.58	NHGIS			
γ_1	College graduation probability coefficient	-3.83	Add Health			
γ_2	College graduation probability coefficient	0.35	Add Health			
γ_3	College graduation probability coefficient	0.15	Add Health			
γ_4	College graduation probability coefficient	1.11	Add Health			

 Table 1: Externally Calibrated Parameters

Notes: The table shows all the externally calibrated parameters.

3.4 Internally Calibrated Parameters

Table 2 lists the remaining twelve parameters that I calibrate by minimizing the sum of squared percentage differences between data and model moments. The data moments include

 $^{^{19}\}mathrm{Appendix}$ Section D.3 provides details on the variable construction, and Appendix Table S4 shows the weighted logit regression estimates.

²⁰I remove eight hours of sleep needs, a standard assumption in the literature.

two measures of household earnings dispersion within commuting zones computed from the ACS 2000: the Gini coefficient of household earnings and the income ratio of non-college and college households. Both are weighted population averages across the 100 biggest commuting zones.²¹ In addition, I ensure that the income and college graduation status relationship matches the data by incorporating the ratio of college-parents share in the first to the fourth quartile of the income distribution. I further include the rank-rank coefficient from Chetty et al. (2014), a coefficient that captures the income correlation between parents and children. It is an inverse measure of social mobility. To discipline the neighborhood quality distribution $(\{m\})$ that directly enters the child skill production function, I use the causal effect of a one standard deviation improvement in neighborhood quality for a child born in the 25th and 75th percentile of the household income distribution estimated by Chetty and Hendren (2018b). I add a Gini coefficient across the ten neighborhoods computed from the NHGIS 2000 dataset to match residential segregation. The place of birth preference parameter is calibrated by matching a moment labeled "residential mobility (D1)". It is defined as the fraction of children born in the first synthetic neighborhood who choose to live in the same synthetic neighborhood in adulthood. To capture parental behaviors, I include parental time by education (displayed in Appendix Table S^2) and household income and education gradients. In addition to discipline parental beliefs, I add the correlation between parents' and children's neighborhood choices.²²

Table 2 reports calibrated parameters, corresponding moments in the data, and their model analogs. Even though every moment results from the combination of all parameters, certain moments are more sensitive to specific parameters. Understanding these intuitive links is informative about the underlying model mechanisms.

The first three parameters are preference parameters and govern parents' choices. In particular, childcare disutility weight κ is pinned down by the fraction of time allocated to childcare by non-college parents, and the preference for place of birth ι is pinned down by residential mobility in the first decile neighborhood. The college wage premium ω directly affects the earnings gap between college and non-college parents.

Neighborhood parameters govern the model geography. In particular, the standard deviation of neighborhood quality σ_m affects how much a child's earnings are affected by neighborhood choices. The relevant moment is the causal effect of neighborhoods measured

²¹The Gini coefficient is lower than typically reported because it is a Gini over twenty years of household income. I compute a yearly Gini coefficient from the data and transform it into a twenty-year Gini coefficient using Shorrocks mobility index estimated by Kopczuk et al. (2010) for 2002.

²²Moments construction and data sources are detailed in Appendix Section D.4.

Parameter	Description	Moment	Data	Model			
Preferences							
b = 0.5	Altruism	Ratio share college parents Q1 to Q4	0.102	0.120			
$\kappa = 0.6$	Parental time disutility	Parental time non-college parents	0.075	0.079			
$\iota = 0.0001$	Place of birth preference	Residential mobility (D1)	0.302	0.274			
$\omega ~=~ 0.005$	College wage premium	Earnings ratio non-college - college	0.554	0.556			
Neighborho	oods						
$\sigma_m = 0.26$	Neighborhood quality	Neighborhood effect (25th pct.)	0.062	0.056			
ν = 0.01	Taste shock variance	Census tract Gini	0.231	0.212			
Skill Forma	Skill Formation: $h' = \left(\left(\gamma \left(\frac{\tau}{\overline{\tau}} \right)^{\varphi} + (1 - \gamma) m^{\varphi} \right)^{\frac{1}{\varphi}} + \underline{i} \right)^{\alpha} h^{1-\alpha} \exp(a')$ with $a' \sim \mathcal{N}(0, \sigma_a)$						
$\alpha = 0.77$	Elasticity of investments	Rank-rank coefficient	0.341	0.339			
$\gamma = 0.55$	Parental time share	Neighborhood effect (75th pct.)	0.046	0.047			
$\varphi = 0.5$	Substitutability	Income gradient in parental time	0.140	0.144			
$\sigma_a = 0.55$	Ability shock variance	Income Gini	0.336	0.334			
Social Lear	ning Process						
μ = 0.3	Update weight	Education parental time gap	0.750	0.850			
$\pi = 0.585$	Cognitive bias strength	Neighborhood quality correlation	0.417	0.460			

 Table 2: Internally Calibrated Parameters

Notes: This table reports the internally calibrated parameters and the observed and simulated moments associated with the parameter estimates.

by Chetty and Hendren (2018b). It determines how much children's future income rank would increase if they had been growing up in one standard deviation better neighborhood. For a child born with a parent at the 25th percentile of the income distribution, the authors find a value of 6.2% of income at the county level within commuting zones. The taste shock variance ν controls residential moves orthogonal to neighborhood quality and affects residential segregation measured by the Gini coefficient across neighborhoods.

The child's skill formation parameters are most relevant for this paper. In particular, the substitutability parameter φ is calibrated by matching the childcare time difference across income groups; here, I use the regression coefficient of parental time on household income quartiles.²³ With social learning and selection neglect, I find that neighborhood quality and parental time are substitute inputs in the child skill production function $\varphi > 0$ (in line with Agostinelli (2018) and Agostinelli et al. (2022)). Parental human capital share $1 - \alpha$ mechanically increases the income correlation between parents and children. Thus, the relevant moment is the rank-rank coefficient between parental and child earnings estimated by Chetty et al. (2014). As ability shock variance captures any income variation not explained by parental choices and human capital, it is calibrated by matching household earnings inequality measured by the income Gini coefficient.

Lastly, the correlation between parents' and children's beliefs is governed by μ and affects the persistence of beliefs and, hence, parental behavior within families. I discipline this parameter by matching the ratio of parental time choices by parents' education levels. This ratio is below one, meaning college parents spend more time with their children than non-college parents. This moment is labeled the education parental time gap. The parental time gradient in education results from two opposing forces in the model. Delusion about the technology of skill formation, if correlated with earnings, increases the gap. However, the substitutability between parental time and neighborhood quality ($\varphi > 0$) and the differential in working hours decrease it. Finally, I calibrate the strength of the selection neglect bias (π) using the correlation between parents' and children's neighborhood choices. Parents' neighborhood choices affect children's future neighborhood decisions through two channels: human capital formation and, hence, earnings and beliefs. Parents' influence on children's earnings is calibrated by matching the rank-rank coefficient and place-based effects. Matching the intergenerational neighborhood correlation ensures a correct discipline of the belief channel. Notice that π is above zero, suggesting that, under the baseline modeling assumptions, selection neglect and the resulting distribution of parental beliefs are needed to match

 $^{^{23}}$ In the data, I control for the gender of the respondent and the age of the child.

aggregate data regarding parental behavior across socioeconomic groups.

3.5 Non-Targeted Moments

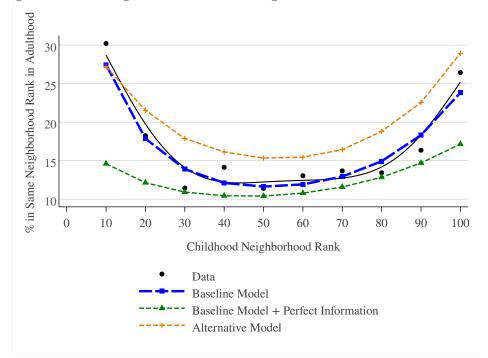


Figure 1: Non-targeted Moments: Intergenerational Residential Mobility

Notes: This Figure shows the share of children who, in adulthood, choose to live in the type of neighborhood as their parents. The dots and solid line are data moments; the baseline model simulated analogs in blue long-dashed-line, the baseline model under perfect information model in green dashed line, and the extended alternative model with perfect information in orange dashed line —data source: Add Health, see Appendix for details of data construction.

The calibrated model matches the targeted moments well and fits the non-targeted residential mobility patterns.²⁴ Figure 1 presents the share of children who live in the same type of neighborhood in adulthood. The solid line is a smooth interpolation between the dots, which are data moments. The blue dashed line represents model simulated analogs. While the first synthetic neighborhood statistic is a targeted moment, the others are not. The model generates a U-shape that is very close to the data. To go further, Figure 2 illustrates a frequency matrix of all possible intergenerational moves, each represented by a colored square. The darker a square is, the more likely a given move. For instance, a child born in

 $^{^{24}\}mathrm{Appendix}$ Section D.5 shows non-targeted moments at the neighborhood level and income quintile matrix.

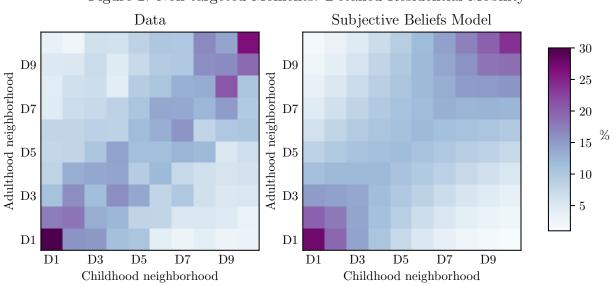


Figure 2: Non-targeted Moments: Detailed Residential Mobility

Notes: This Figure shows residential mobility between childhood and adulthood in the data (left panel), and their model simulates analogs (right panel). The x-axis contains the ten synthetic childhood neighborhoods, and the y-axis is the ten synthetic adulthood neighborhoods. The frequency of moves is represented by cell colors, with larger values in darker squares—data source: Add Health, see Appendix D.4 for details of data construction.

Neighborhood one is likely to live in Neighborhood one or two when she becomes an adult, but she is unlikely to live in Neighborhood six or above. The calibrated model (right panel) matches the data patterns (left panel) remarkably well.

3.6 Discussion of the Social Learning Channel

The model is calibrated under social learning at the neighborhood level with potential selection neglect. I find a selection neglect bias strength parameter higher than zero (0.585), suggesting that, under the baseline modeling assumptions, imperfect information is needed to match aggregate data regarding parental behavior across socioeconomic groups. Natural questions are: What is the impact of the endogenous distribution of beliefs on the economy? And how well would the model do under perfect information?

3.6.1 The Role of Parental Beliefs

I first shut down the selection neglect channel ($\pi = 0$) to understand parental beliefs' role in the economy. This means, I now assume parents are perfectly aware of the relevance of parental inputs (α), and I solve for the general equilibrium under the current calibration but π . Table 3 presents the differences in outcomes between the baseline economy and one with perfect information ($\pi = 0$).

Providing full information would lead parents in the bottom quartile of the income distribution to update their beliefs about the relevance of parental inputs upward by 17% and parents in the top quartile of the income distribution to update them downward by 7%. These numbers are of a reasonable order of magnitude. Cunha et al. (2013), who elicits disadvantaged African American mothers' beliefs about the elasticity of child development with respect to parental investments, finds greater differences between the truth and their beliefs. As a result, low-income parents allocate too little time to their children's education, while high-income parents allocate too much time. Providing information to parents would, in general, increase low-income households' parental time by 31% and decrease high-income households' one by 5%. Under perfect information, aggregate parental time increases by 7.5%. Parents' distorted beliefs decrease social mobility—negative rank-rank coefficient and earnings by 12% and 3% respectively and increase inequality and poverty by 3% and 17%.²⁵ The green dashed line in Figure 1 depicts intergenerational residential mobility under perfect information with the baseline calibration. It shows that social learning and parental beliefs almost double the share of children born in the bottom-quality neighborhood who choose to reside in bottom-quality neighborhood in adulthood. With perfect information, aggregate welfare, defined by the consumption equivalence under the veil of ignorance in the baseline economy relative to the counterfactual economy, would increase by 0.6%, with a more substantial effect for the lowest-income households. To summarize, I find a relatively modest level of delusion, coherent with micro-studies, that has large effects on the economy.

 $^{^{25}}$ Poverty is measured by the absolute level of poverty. The poverty threshold is defined at baseline by the tenth percentile of the household income distribution.

		Household Income quartile			
	All	1st	2nd	3rd	4th
Subjective Beliefs	+2.8%	+17.5%	+5.9%	-0.2%	-7.4%
Parental Time	+7.5%	+30.9%	+9.9%	+2.5%	-4.8%
Earnings	+2.5%	+6.4%	+5.8%	+4.7%	+2.2%
Rank-rank coefficient (Social immobility)	-11.8%				
Census tract Gini (Segregation)	-0.6%				
Income Gini (Inequality)	-2.7%				
Absolute poverty	-16.9%				
Welfare	+0.58%	+0.88%	+0.54%	+0.47%	+0.46%

Table 3: Providing Information - Effects of Subjective Beliefs

Notes: This table displays percentage differences in model-generated moments between the baseline calibrated model with and without subjective beliefs.

3.6.2 Alternative Modeling under Perfect Information

Which moments would a perfect information model miss? I first re-calibrate the same model assuming perfect information by shutting down the selection neglect bias channel ($\pi = 0$). Unsurprisingly, and despite a good match of social mobility and inequality moments, appendix Table S6 shows a relatively bad fit for all untargeted moments.²⁶ The fact that in the baseline model, the selection neglect bias strength parameter is higher than zero already indicates that a perfect information model needs an additional mechanism that drives heterogeneity in parental input choices. Notice, however, that two parental behavior moments targeted at baseline are not, which renders the comparison of the two calibrated models somewhat unfair.

In the second step, I augment the alternative model with heterogeneous preferences regarding the altruism parameter and quadratic moving costs. This extension provides two extra free parameters and mechanically generates heterogeneity in parental input choices by socioeconomic group. Parents' preferences take the following form:

 $^{^{26}}$ Appendix Figures S4 and S5 show the other non-targeted moments. The intergenerational residential mobility moments are all off. In particular, in the mobility matrix under perfect information, not only is the diagonal too dark but all the squares off-diagonal are of similar color, which contrasts with the data.

$$\log(c) + \frac{(1 - \overline{\ell_s} - \kappa \tau)^{1 - \frac{1}{\psi}}}{1 - \frac{1}{\psi}} + \iota \mathbb{1}_{m_0 = m} - \xi (m_0 - m)^2 + \nu \varepsilon_m + b_s \mathbb{E} \left[\mathcal{V}(h', s', m, \alpha) \right],$$

with b_s , the altruism parameter that now depends on the college education status s, capturing a difference for the valuation of children's future outcomes by education. Even though the empirical literature provides no evidence of such an altruism gap, it could generate a differential in parental time by education status. The quadratic moving costs are governed by ξ and suggest a homophily bias for neighborhood quality types. Two parents of similar earnings and similar taste shocks could have different preferences for living in a neighborhood depending on how close was their childhood neighborhood quality type compared to the current one. This last feature mechanically creates a U-shape in residential mobility and a smooth gradient in the frequency matrix of intergenerational residential moves.

Appendix Table S7 shows a relatively good fit of this augmented alternative model with one exception: the positive correlation between income and parental time is too weak. With perfect information, the positive correlation between parental time and income is driven by the complementarity between parental time and neighborhood quality in the technology of skill formation ($\varphi < 0$). However, despite having $\varphi = -5$ very negative, this alternative model does not capture the income gradient in parental time well–it is 0.106 instead of 0.14.

The analysis of the untargeted intergenerational residential mobility moments is disappointing. As expected, the quadratic moving costs mechanically generate a U-shape pattern in residential mobility, but it is upward-shifted (c.f. Figure 1 orange dashed line). The reason lies in the preference parameter ι . Comparing Appendix Table S7 and Table 2, notice that to have 30% of children born in the bottom-quality neighborhood who stay in the alternative model, the preference parameter ι needs to be much larger than in the baseline model. However, this feature reduces mobility in all other neighborhoods.

These results imply that with perfect information, additional types of heterogeneity are needed to match the data. In addition to quadratic moving costs and differences in altruism parameters, the preference for the neighborhood should vary by childhood neighborhood (ι_{m_0}) . Appendix Figure S6 shows targeted intergenerational mobility moments with this alternative model that includes heterogeneity in the preference for the neighborhood. In particular, to reproduce the U-shape data patterns in residential mobility, the preference for childhood neighborhoods needs to be about thirty times higher in the bottom-quality neighborhood than in the middle-quality ones.

While preference heterogeneity can help match the data, its origin is difficult to justify. Does altruism for children systematically differ by education status? How does it transmit to the next generation? Are quadratic moving costs credible? Why would children born in the bottom quality neighborhood be so much more attached than others to their neighborhood quality given the negative features it has: high crime rates, high poverty rates, a low opportunity for children?²⁷ This last feature is at odds with Bergman et al. (2019)'s empirical findings. The authors compare low-income families randomly allocated between treatment and control groups. Parents in the treatment group are induced to move to higher-quality neighborhoods. They find that those parents are more likely to be satisfied and willing to stay in their new neighborhood than those in the control group. Discrimination or a homophily bias could motivate other modeling assumptions. However, the fact that Bergman et al. (2019) find higher satisfaction levels of low-income families who moved to higher-quality neighborhoods suggests that if they face discrimination once installed, it does not make them systematically want to move back to low-quality neighborhoods. In Appendix Table S8, I find that while childhood neighborhood quality is correlated with adulthood neighborhood quality, once controlled for childhood neighborhood quality, race is not the primary driver of intergenerational residential mobility.

4 Housing Voucher Policies

The baseline model displays two main frictions that motivate government involvement: parents cannot borrow against their children's future earnings and information frictions that result from segregation and selection neglect. Both lead to lower levels of parental inputs, including lower neighborhood quality, in low-income families compared to a perfect information world in which children could control inputs into their development.

In this section, I use the quantitative model to study the effects of housing vouchers. The Housing Choice Voucher program in the U.S. aims to promote the mobility of low-income families.²⁸ The model provides a new rationale for this policy. In addition to addressing redistribution concerns, this policy can improve information about the child skill technology in the economy by reducing segregation.

²⁷Commuting costs are not explicitly modeled but captured by the idiosyncratic neighborhood taste shocks. However, they are unlikely to explain residential mobility patterns across neighborhood quality. Indeed Chetty and Hendren (2018a) find no correlation between short commute time and place effects on children's future earnings.

²⁸https://www.huduser.gov/quarterly_update/update_June2015.html

In the model, housing vouchers are financed through property taxes, which adds two terms to the household budget constraint:

$$c + r_{m,h,s}^{HV} \left(1 + \tau_r\right) = w \ h \left(1 + \omega s\right) \overline{\ell_s} + R,$$

where τ_r is the tax rate and $r_{m,h,s}^{hv}$, is the rent households face once the housing voucher policy is implemented. The government budget constraint is balanced such that:

$$\sum_{m} \sum_{s} \int (r_m - r_{m,h,s}^{HV}) F(h,s,m) \, dh = \sum_{m} \sum_{s} \int (r_{m,h,s}^{HV} \tau_r) F(h,s,m) \, dh.$$

4.1 Housing Voucher Policy

The Housing Choice Voucher program rule imposes that seventy-five percent of families who receive housing vouchers each year have "extremely low incomes," defined as incomes up to the poverty line. The others' income may not exceed 50% of the median income for the metropolitan area where the family chooses to live. The voucher generally covers the difference between 30 percent of the family income and the rent, up to a limit based on Housing and Urban Development's fair market rent estimates at the metropolitan area level.

I consider a housing voucher policy closely designed as the Housing Choice Voucher program. Housing vouchers are offered to young parents before they make their residential choice. The vouchers cover the difference between 30% of the family's income and the rent up to the rent ceiling, the 40th percentile rent in the commuting zone. Eligible households are those below the poverty threshold, defined as the income level at the tenth percentile of the income distribution. Let r_{m40} the 40th percentile rent in the commuting zone, then the rent price in the neighborhood m for a parent of income y(h, s) who is eligible for the housing voucher is:

$$r_{m,h,s}^{HV} = \min(0.3 \times y(h,s), r_m) + \max(r_m - r_{m40}, 0).$$

As a first step, I conduct a field experiment within the model to investigate the impact of housing vouchers and compare them to the empirical estimates by Chetty et al. (2016). These are partial equilibrium results, as, in practice, too few people are treated to change equilibrium forces. Then, I scale up the policy without changing the eligibility criterion and consider steady-state comparisons, which helps gauge the long-run implications.

4.1.1 Randomized Control Trial Within Model

Column 4 Table 4 shows the positive effects of housing vouchers on eligible households. The housing voucher policy improves neighborhood rank by 1.5 points for treated families, improving children's earnings at age 26 by \$663. The predicted effect on children's earnings falls within Chetty et al. (2016)'s estimated confidence interval (\$1,452 with a standard error of 736).²⁹ The policy induces an extra 62% of families to move out of bottom-quality neighborhoods in the data and the model.

Incorrect parental beliefs are part of why not all low-income families move to high-quality neighborhoods. In Column 5 Table 4, I conduct the same experiment but provide information about the returns to neighborhood quality to treated families. The neighborhood rank of treated families improves by 1.9 points, 0.4 points higher than with only housing vouchers. As a result, perfect information further increases treated children's adulthood earnings by \$132. Notice here that the fraction of families who move out of bottom-quality neighborhoods with information rises to 76%. The number does not reach 100%, suggesting that preferences partly explain why not all families leave deprived neighborhoods when receiving housing vouchers and information, which is consistent with Bergman et al. (2019)'s findings. The authors randomly provided services to reduce barriers to moving to high-upward-mobility areas, such as information, customized search assistance, landlord engagement, and shortterm financial assistance. Although the intervention increased the fraction of families who moved to high-upward-mobility areas, this number did not reach 100%.

4.1.2 Scaling-up Housing Vouchers

In the next step, I scale up the policy to all families below the poverty threshold in the economy and compute the new steady state. The steady-state comparisons provide insights into the long-run implications of the policy.

General equilibrium responses in rents and beliefs amplify housing voucher effects on eligible households. While Column 1 of Table 5 repeats the partial equilibrium effects of the housing voucher policy on eligible families, Column 2 shows the long-run effects of the same policy that is scaled up. Compared to partial equilibrium, long-run effects on eligible

²⁹Notice that the estimated effect is in the lower bound of Chetty et al. (2016)'s empirical estimate. This is most likely because treated individuals are poorer in the data than in the model. Indeed, while Chetty et al. (2016) evaluate housing vouchers' effects on low-income households who already live in public housing in deprived neighborhoods, in the model, the voucher is offered to young parents with an income below the poverty rate, independently of their neighborhood choice. Only 40% of them choose to live in the very bottom decile neighborhood. As a result, in the data, the average family earnings at age 26 of children in the control group is \$12,702, while in the model, it is \$20,917.

		Data	Model			
	Control Housing Vouchers		Control	Housing Vouchers	Housing Vouchers + Info	
	(1)	(2)	(3)	(4)	(5)	
% in bottom-quality neighborhood	100%	[-62%; -70%]	40%	-62%	-76%	
Children's future earnings	\$12,702	[+\$11;+\$2,893]	\$20,917	+\$663	+\$795	
Neighborhood rank			2.14	+1.5	+1.9	
Parental time (min./day)			57	+1	+1	

Table 4: Effects of a Housing Voucher Policy on Eligible Households

Notes: This table shows the effects of housing vouchers on eligible families, from the data, and simulated by the calibrated baseline model. Data source: Chetty et al. (2016).

households' parental time and neighborhood rank are more prominent (+1.6 versus +1.5 and +9 versus +1, respectively), further increasing eligible children's earnings by +\$1,008 per year (\$1,671 versus \$663).

In the long run, the housing voucher policy has overall positive effects. Column 3 of Table 5 shows the policy effects on all households. With housing vouchers, earnings at age 26 increase by \$277, and inequality, poverty, and the rank-rank coefficient decrease. This suggests that housing vouchers benefit eligible households and can help combat segregation's adverse effects on inequality and intergenerational mobility.

I fix information frictions at its baseline level to understand whether the long-run effects of housing vouchers are due to the housing market response or a change in information frictions. The policy effects presented in Columns 4 and 5 of Table 5 can be considered short- or medium-run policy effects, as only the housing market response is considered. Partial equilibrium effects on eligible children's earnings are amplified, but only by \$207 per year (\$870 versus \$663). This moderate amplification effect is driven by an increase in neighborhood rank due to the voucher and the housing market response but an absence of improvement in parental time. This suggests that most—about 80%—of the amplification effect on eligible households results from a change in information frictions.

Ignoring the shift in information frictions might lead to different conclusions depending on the policy maker's objectives (Columns 5 of Table 5). If only the housing market reacts, but the distribution of parental beliefs remains unchanged, inequality and poverty increase while earnings and social mobility decrease. Figure 3 and Table 6 help understand

	Small Field	Large Scale and Long Run			
	Baseline model	Baseline model		Baseline model without change in social learning	
Households	Eligible (1)	Eligible (2)	All (3)	Eligible (4)	All (5)
% in neighborhood D1 Children's future earnings Neighborhood rank Parental time (min./day)	-62% +\$663 +1.5 +1	-58% +\$1,671 +1.6 +9	-3% +\$277 +0.0 +2	-69% + +\$870 +1.9 +0	-1% -\$57 +0.0 -1
Inequality Poverty Earnings Rank-rank coefficient			-0.8% -6.3% +0.9% -3.8%		+0.0% +1.3% -0.2% +0.5%

Table 5: The Effects of Scaling-up Housing Vouchers

Notes: This table shows the effects of scaling-up housing vouchers within the calibrated baseline model.

parental beliefs' role in the long-run policy effects. In the long run, the distribution of parental beliefs evolves. Eligible households move to higher-rank neighborhoods, improving parents' beliefs, particularly those of low-income parents. This leads to a change in parents' behavior. Low-income parents spend more time with their children despite an increase in neighborhood quality (remember that neighborhood quality and parental time are substitute inputs in the technology of skill formation). The change in parental beliefs decreases the share of parents in the bottom-quality neighborhood and improves the share of parents in higher-quality neighborhoods (Figure 3). As a result, social mobility improves, and inequality decreases. However, all those positive effects are absent when ignoring the change in information frictions.

A perhaps surprising effect of the policy is the absence of a decrease in high-income households' beliefs (Column 5 Table 6). Decreased segregation should improve information, decreasing the parental beliefs of high-income parents who overestimate the relevance of parental inputs. The reason is that the policy has a unique rent ceiling for the commuting zone, which creates a bunching at the rent limit. This bunching is illustrated by the peak in neighborhood 5 in Figure 3 and observed in the data by Collinson and Ganong (2018). As a result, low-income households don't move to the highest-quality neighborhoods, and information does not improve in those neighborhoods. Since there is a debate concerning the

		Household Income quartile				
	All 1st 2nd 3rd 4th					
Δ Parental Beliefs	+2.8%	+7.1%	+3.3%	+2.2%	+0.2%	
Δ Parental Time	+2.6%	+8.0%	+2.2%	+1.2%	+1.3%	
Δ Earnings	+0.9%	+0.7%	+2.3%	+3.5%	+2.3%	
Δ Welfare	+0.29%	+1.27%	+0.03%	-0.04%	-0.05%	

Table 6: The Effects of Scaling-up Housing Vouchers by Income Quartile

Notes: This table shows the effects of scaling-up housing vouchers by income group.

unique rent feature of the Housing Choice Voucher program, I evaluate a housing voucher policy with rent limits set at the neighborhood level instead of at the commuting zone level.

4.2 Housing Voucher Policy with Rent Limits Indexed at the Neighborhood Level

Since Chetty et al. (2016) provided evidence that housing vouchers effectively improve adulthood earnings through improved neighborhood quality, the United States Department of Housing and Urban Development has put additional effort into promoting high-quality mobility. In particular, since 2019, the Department of Housing and Urban Development has allowed housing agencies to set voucher subsidies at local rents rather than at the metro area level.³⁰ This decision addresses an issue raised about unique rent ceilings: they do "not adequately help families access low-poverty neighborhoods."³¹ Indeed, Collinson and Ganong (2018) finds that most rental units below the payment standard are in low-quality neighborhoods. Indexing rent limits to ZIP codes rather than metropolitan areas improves the share of families who move into higher-quality neighborhoods.

4.2.1 Housing Voucher Policy with Multiple Rent Limits

I consider a housing voucher policy designed to mimic the Housing Choice Voucher program but with rent limits defined at the neighborhood level. Since the model does not feature heterogeneity in neighborhood rents, rent limits are determined by the median rent in each neighborhood. As before, eligible households are those below the poverty threshold, defined as the income level at the tenth percentile of the income distribution.

³⁰https://www.cbpp.org/research/housing/what-are-housing-mobility-programs-and-why-are-they-needed
³¹https://www.huduser.gov/portal/pdredge/pdr_edge_frm_asst_sec_061515.html

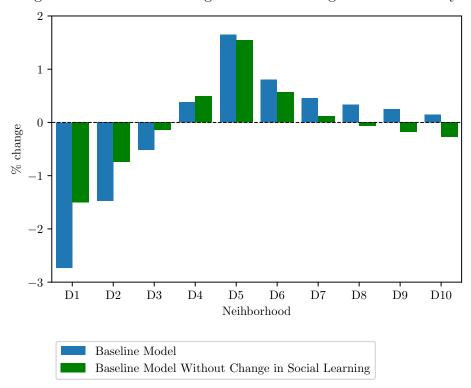


Figure 3: Effects of Housing Vouchers on Neighborhood Density

 $\it Notes:$ This Figure shows the long-run change in neighborhood density due to the scaled-up housing voucher policy.

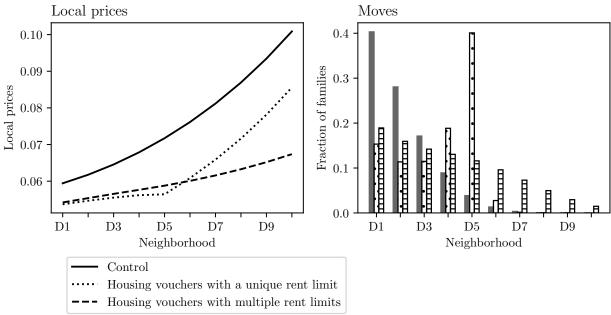


Figure 4: Design of Housing Voucher Policies - Eligible Households - Partial Equilibrium

Notes: The left panel of this Figure shows the rent schedule for an average eligible household under three scenarios: no policy (control), housing vouchers with a unique rent limit, and housing vouchers with multiple rent limits. The right panel of this Figure shows the residential choices of eligible households under the three scenarios.

Housing vouchers cover the difference between a fraction of the family's income and a fraction of the median rent in each neighborhood. Those fractions are defined so that (i) in partial equilibrium, the cost of the policy is the same as the cost of a housing voucher with a unique rent limit, and (ii) the rent faced by an average eligible household is the same across the two policies in the first neighborhood. Under this new housing voucher policy, housing vouchers cover the difference between 70.5% of the median rent and 20% of the family income in each neighborhood. Under this new housing voucher policy (NHV), the rent price in the neighborhood m for a parent of income y(h, s) who is eligible for the housing voucher is:

$$r_{m,h,s}^{NHV} = \min(0.2 \times y(h,s) + 0.295 * r_m, r_m)$$

The left panel of Figure 4 illustrates the rent schedule of this new policy for an average eligible household. While the rent schedule has a kink under a housing voucher policy with a unique rent limit, it is smooth under a housing voucher policy with rent limits set at the neighborhood level.

4.2.2 Effects of a Housing Voucher Policy with Multiple Rent Limits

Partial Equilibrium Effects of the Policy. Consistent with Collinson and Ganong (2018)'s empirical findings, I find that a housing voucher policy with multiple rent limits further improves the neighborhood rank of eligible households even though more families choose to live in the bottom quality neighborhood (right panel of Figure 4 and Column 1 Table 7). As a result, the effect on children's future earnings is more substantial than under a unique rent limit housing voucher policy, with an increase of \$809 per year at age 26.

	Small Field Large Scale and I		and Long Run
	Baseline model	Baseline model	
Households	Eligible (1)	Eligible (2)	All (3)
% in bottom-quality neighborhood	-53%	-69%	-3%
Children's future earnings	+\$809	+\$2,477	-\$1
Neighborhood rank	+1.8	+3.3	+0.0
Parental time (min./day)	+1	+10	-1
Inequality			-1.5%
Poverty			-6.2%
Earnings			-0.0%
Rank-rank coefficient			-8.5%

Table 7: The Effects of Scaling-up Housing Vouchers with Multiple Rent Limits

Notes: This table shows the effects of scaling-up housing vouchers with multiple rent limits within the calibrated baseline model.

Large Scale and Long-run Effects of the Policy. Column 3 of Table 8 shows that general equilibrium responses in local prices and beliefs greatly amplify the effects of the policy on eligible households. The neighborhood rank is much higher than under a policy with a unique rent limit (3.3 versus 1.6), increasing children's future earnings by \$2,477 per year—the difference in amplification effects between the two policies mainly results from improved housing market access. The attractiveness of the bottom-quality neighborhood decreases even further, as depicted in Figure 5, while the attractiveness of very high-quality neighborhoods increases. Parental beliefs of low-income families increase under both policy regimes (Column 2 of Tables 6 and 8).

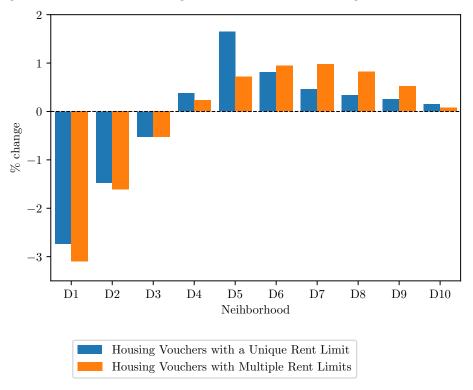
The housing voucher policy with multiple rent limits also positively affects the economy. Column 3 of Table 7 shows the policy effects on all households. This policy substantially affects inequality and social mobility (+1.5%, +8.5%, respectively). However, the effects

		Household Income quartile			
	All	1st	2nd	3rd	4th
Δ Parental Beliefs	-0.3% -1.1%	+6.6% +7.8%	+0.9% -0.6\%	-1.7%	-4.8% -5.1%
Δ Parental Time Δ Earnings	-1.1% -0.0%	+7.8% +0.7%	, ,	-3.2% +1.9%	-5.1% -0.6%
Δ Welfare	+0.24%	+1.17%	+0.00%	-0.07%	-0.08%

Table 8: The Effects of Scaling-up Housing Vouchers with Multiple Rent Limits by Income Quartile

Notes: This table shows the effects of scaling-up housing vouchers with multiple rent limits by income group.

Figure 5: Effects of Housing Voucher Policies on Neighborhood Density



Notes: This Figure shows the long-run change in neighborhood density due to the scaled-up housing voucher policies.

on earnings and, consequently, on absolute poverty and welfare are weaker. Figure 5 and Table 8 help understand the underlying reasons. Under the housing voucher policy with multiple rent limits, eligible households have better access to all neighborhoods, decreasing segregation and improving information everywhere. In the long run, parents' beliefs become closer to the truth, increasing the parental beliefs of low-income parents but decreasing those of high-income parents. This leads to a change in parents' behavior across the entire income distribution. Low-income parents spend more time with their children (+8%), and high-income parents spend less time with their children (-5%). As a result, average parental time decreases (-1%), and earnings do not improve. However, the policy significantly affects social mobility and inequality as it mitigates the distorting effects of parents' beliefs.

In sum, a housing voucher policy with multiple rent limits is a better tool to address redistribution concerns and improve information, mitigating the distorting effect of parental beliefs than a housing voucher policy with a unique rent limit. However, in the long run, because it decreases high-income parents' beliefs, this policy does not enhance aggregate income, having a somewhat weaker effect on aggregate welfare compared to the previous policy.³²

5 Conclusion

In this paper, I present a quantitative spatial model of residential and parental time decisions with social learning about the technology of skill formation and potential selection neglect. Once calibrated to the average commuting zone in the United States, the baseline model has residential segregation generating information frictions that shape parental beliefs and distort parental input choices. In equilibrium, while low-income parents underestimate the relevance of parental inputs for the child's development, high-income parents overestimate it. Introducing endogenous parental beliefs helps rationalize two surprising parental behaviors across socioeconomic groups: parents raised in the worse neighborhoods tend to raise their children in the same type of neighborhoods, and college parents, despite working more hours, tend to allocate more active time to their children's education than non-college parents. While heterogeneous preferences by socioeconomic groups could rationalize those data patterns, I find that they would need to be rather large and are difficult to defend for some of them empirically.

 $^{^{32}}$ Although it is a standard welfare measure in the literature, consumption equivalence welfare captures the trade-off between efficiency and inequality within cohorts but does not internalize improvements in intergenerational mobility.

Using the baseline calibrated model, I investigate the effects of parental beliefs on the United States economy. Relatively modest levels of parental delusion have significant macroeconomic effects as they increase inequality and decrease social mobility and aggregate earnings, reducing consumption equivalence welfare. A housing voucher policy that induces lowincome households to move to higher-quality neighborhoods improves welfare in the long run. Indeed, the model predicts positive impacts on the economy, as a housing voucher program can decrease residential segregation in general equilibrium, leading to a shift in parental beliefs in the long run, reducing inequality and poverty and increasing social mobility.

References

- Adam, K., Marcet, A., and Beutel, J. (2017). Stock price booms and expected capital gains. American Economic Review, 107(8):2352–2408.
- Agostinelli, F. (2018). Investing in children's skills: An equilibrium analysis of social interactions and parental investments. Unpublished Manuscript, University of Pennsylvania.
- Agostinelli, F., Doepke, M., Sorrenti, G., and Zilibotti, F. (2022). When the great equalizer shuts down: Schools, peers, and parents in pandemic times. *Journal of public economics*, 206:104574.
- Ahlfeldt, G. M., Redding, S. J., Sturm, D. M., and Wolf, N. (2015). The economics of density: Evidence from the berlin wall. *Econometrica*, 83(6):2127–2189.
- Alan, S., Boneva, T., and Ertac, S. (2019). Ever failed, try again, succeed better: Results from a randomized educational intervention on grit. *The Quarterly Journal of Economics*, 134(3):1121–1162.
- Algan, Y., Bouguen, A., Chevallier, C., and Charpentier, A. (2020). The impact of a largescale mindset intervention on school outcomes: Experimental evidence fromfrance. Working paper.
- Attanasio, O., Boneva, T., and Rauh, C. (2019). Parental beliefs about returns to different types of investments in school children. Working Paper 25513, National Bureau of Economic Research.
- Attanasio, O. P. and Kaufmann, K. M. (2014). Education choices and returns to schooling: Mothers' and youths' subjective expectations and their role by gender. *Journal of Development Economics*, 109:203–216.
- Belfield, C., Boneva, T., Rauh, C., and Shaw, J. (2019). What drives enrolment gaps in further education? the role of beliefs in sequential schooling decisions. *Economica*.
- Bénabou, R. and Tirole, J. (2005). Self-confidence and personal motivation. Psychology, Rationality and Economic Behaviour: Challenging Standard Assumptions, pages 19–57.
- Bergman, P., Chetty, R., DeLuca, S., Hendren, N., Katz, L. F., and Palmer, C. (2019). Creating moves to opportunity: Experimental evidence on barriers to neighborhood choice. Working Paper 26164, National Bureau of Economic Research.

- Bilal, A. (2021). The geography of unemployment. Working Paper 29269, National Bureau of Economic Research.
- Blandin, A. and Herrington, C. (2022). Family heterogeneity, human capital investment, and college attainment. *American Economic Journal: Macroeconomics*, 14(4):438–78.
- Boneva, T. and Rauh, C. (2016). Human capital production and parental beliefs. Unpublished Manuscript, University College London.
- Boneva, T. and Rauh, C. (2018). Parental beliefs about returns to educational investments—the later the better? *Journal of the European Economic Association*, 16(6):1669– 1711.
- Breda, T., Grenet, J., Monnet, M., and van Effenterre, C. (2019). Female Role Models: are they effective at encouraging girls to study science? IPP Policy Brief n°45, Institut des politiques publiques.
- Caucutt, E. M., Lochner, L., and Park, Y. (2017). Correlation, consumption, confusion, or constraints: Why do poor children perform so poorly? The Scandinavian Journal of Economics, 119(1):102–147.
- Chetty, R. and Hendren, N. (2018a). The impacts of neighborhoods on intergenerational mobility i: Childhood exposure effects. *The Quarterly Journal of Economics*, 133(3):1107– 1162.
- Chetty, R. and Hendren, N. (2018b). The impacts of neighborhoods on intergenerational mobility ii: County-level estimates. The Quarterly Journal of Economics, 133(3):1163– 1228.
- Chetty, R., Hendren, N., and Katz, L. F. (2016). The effects of exposure to better neighborhoods on children: New evidence from the moving to opportunity experiment. *American Economic Review*, 106(4):855–902.
- Chetty, R., Hendren, N., Kline, P., Saez, E., and Turner, N. (2014). Is the united states still a land of opportunity? recent trends in intergenerational mobility. *American Economic Review*, 104(5):141–47.
- Chetty, R., Jackson, M. O., Kuchler, T., Stroebel, J., Hendren, N., Fluegge, R. B., Gong, S., Gonzalez, F., Grondin, A., Jacob, M., Johnston, D., Koenen, M., Laguna-Muggenburg,

E., Mudekereza, F., Rutter, T., Thor, N., Townsend, W., Zhang, R., Bailey, M., Barberá,P., Bhole, M., and Wernerfelt, N. (2022). Social capital i: measurement and associations with economic mobility. *Nature*.

- Chyn, E. (2018). Moved to opportunity: The long-run effects of public housing demolition on children. *American Economic Review*, 108(10):3028–56.
- Chyn, E. and Daruich, D. (2022). An equilibrium analysis of the effects of neighborhoodbased interventions on children. Working Paper 29927, National Bureau of Economic Research.
- Collinson, R. and Ganong, P. (2018). How do changes in housing voucher design affect rent and neighborhood quality? *American Economic Journal: Economic Policy*, 10(2):62–89.
- Conley, T. G. and Udry, C. R. (2010). Learning about a new technology: Pineapple in ghana. *American economic review*, 100(1):35–69.
- Cunha, F., Elo, I., and Culhane, J. (2013). Eliciting maternal expectations about the technology of cognitive skill formation. Working Paper 19144, National Bureau of Economic Research.
- Cunha, F. and Heckman, J. (2007). The technology of skill formation. American Economic Review, 97(2):31–47.
- Cunha, F. and Heckman, J. J. (2009). The economics and psychology of inequality and human development. *Journal of the European Economic Association*, 7(2-3):320–364.
- Cunha, F., Heckman, J. J., and Schennach, S. M. (2010). Estimating the technology of cognitive and noncognitive skill formation. *Econometrica*, 78(3):883–931.
- Daruich, D. (2018). The macroeconomic consequences of early childhood development policies. Working Paper 2018-29, FRB St. Louis.
- Das, J., Dercon, S., Habyarimana, J., Krishnan, P., Muralidharan, K., and Sundararaman, V. (2013). School inputs, household substitution, and test scores. *American Economic Journal: Applied Economics*, 5(2):29–57.
- Diamond, R. (2016). The determinants and welfare implications of us workers' diverging location choices by skill: 1980-2000. American Economic Review, 106(3):479–524.

- Dizon-Ross, R. (2019). Parents' beliefs about their children's academic ability: Implications for educational investments. *American Economic Review*, 109(8):2728–65.
- Doepke, M., Hannusch, A., Kindermann, F., and Tertilt, M. (2022). The economics of fertility: A new era. Working Paper 29948, National Bureau of Economic Research.
- Durlauf, S. N. (2011). Chapter 6. Groups, Social Influences, and Inequality, pages 141–175. Princeton University Press.
- Eckert, F., Kleineberg, T., et al. (2019). Can we save the american dream? a dynamic general equilibrium analysis of the effects of school financing on local opportunities. In 2019 Meeting Papers, number 1197. Society for Economic Dynamics.
- Enke, B. (2020). What you see is all there is. *The Quarterly Journal of Economics*, 135(3):1363–1398.
- Fernández, R. (2013). Cultural change as learning: The evolution of female labor force participation over a century. American Economic Review, 103(1):472–500.
- Fogli, A. and Guerrieri, V. (2019). The end of the american dream? inequality and segregation in us cities. Working Paper 26143, National Bureau of Economic Research.
- Fogli, A. and Veldkamp, L. (2011). Nature or nurture? learning and the geography of female labor force participation. *Econometrica*, 79(4):1103–1138.
- Frick, M., Iijima, R., and Ishii, Y. (2022). Dispersed behavior and perceptions in assortative societies. American Economic Review, 112(9):3063–3105.
- Fuchs-Schündeln, N., Krueger, D., Ludwig, A., and Popova, I. (2022). The long-term distributional and welfare effects of covid-19 school closures. *The Economic Journal*, 132(645):1647–1683.
- Gregory, V., Kozlowski, J., and Rubinton, H. (2022). The impact of racial segregation on college attainment in spatial equilibrium. Working Paper 2022-36, FRB St. Louis Working Paper.
- Guryan, J., Hurst, E., and Kearney, M. (2008). Parental education and parental time with children. *Journal of Economic Perspectives*, 22(3):23–46.
- Guyon, N. and Huillery, E. (2020). Biased Aspirations and Social Inequality at School: Evidence from French Teenagers. *The Economic Journal*.

- Heckman, J. J. and Mosso, S. (2014). The economics of human development and social mobility. Annual Review of Economics, 6(1):689–733.
- Hofferth, S. L., Flood, S. M., Sobek, M., and Backman, D. (2020). American time use survey data extract builder: Version 2.8 [dataset]. College Park, MD: University of Maryland and Minneapolis, MN: IPUMS.
- Hwang, Y. (2022). Neighborhood effects on intergenerational cultural transmission. Working Paper 4017952, SSRN.
- Jang, Y. and Yum, M. (2020). Aggregate and Intergenerational Implications of School Closures: A Quantitative Assessment. Discussion Paper Series 234v1, CRC TR 224.
- Jehiel, P. (2018). Investment strategy and selection bias: An equilibrium perspective on overoptimism. American Economic Review, 108(6):1582–97.
- Jensen, R. (2010). The (perceived) returns to education and the demand for schooling. *The Quarterly Journal of Economics*, 125(2):515–548.
- Kaufmann, K. M. (2014). Understanding the income gradient in college attendance in mexico: The role of heterogeneity in expected returns. *Quantitative Economics*, 5(3):583–630.
- Kiessling, L. (2021). How do parents perceive the returns to parenting styles and neighborhoods? *European Economic Review*, 139:103906.
- Kim, S., Tertilt, M., and Yum, M. (2021). Status externalities in education and low birth rates in korea. Discussion Paper No. 16271, CEPR Press.
- Kling, J. R., Liebman, J. B., and Katz, L. F. (2001). Bullets don't got no name: Consequences of fear in the ghetto. Working paper, JCPR.
- Kopczuk, W., Saez, E., and Song, J. (2010). Earnings inequality and mobility in the united states: evidence from social security data since 1937. *The Quarterly Journal of Economics*, 125(1):91–128.
- Lee, S. Y. and Seshadri, A. (2019). On the intergenerational transmission of economic status. Journal of Political Economy, 127(2):855–921.
- Manson, S., Schroeder, J., Van Riper, D., Kugler, T., and Ruggles, S. (2022). Ipums national historical geographic information system: Version 17.0 [dataset]. *Minneapolis, MN: IPUMS.*

- Nakamura, E., Sigurdsson, J., and Steinsson, J. (2022). The gift of moving: Intergenerational consequences of a mobility shock. *The Review of Economic Studies*, 89(3):1557–1592.
- Nguyen, T. (2008). Information, role models and perceived returns to education: Experimental evidence from madagascar. *Unpublished manuscript*, 6.
- Pop-Eleches, C. and Urquiola, M. (2013). Going to a better school: Effects and behavioral responses. American Economic Review, 103(4):1289–1324.
- Redding, S. J. and Rossi-Hansberg, E. (2017). Quantitative spatial economics. Annual Review of Economics, 9:21–58.
- Roemer, J.-E. and Wets, R.-J.-B. (1994). Neighborhood Effects on Belief Formation and the Distribution of Education and Income. Papers 94-02, California Davis - Institute of Governmental Affairs.
- Streufert, P. (2000). The effect of underclass social isolation on schooling choice. Journal of Public Economic Theory, 2(4):461–482.
- Tauchen, G. (1986). Finite state markov-chain approximations to univariate and vector autoregressions. *Economics letters*, 20(2):177–181.
- Wiswall, M. and Zafar, B. (2021). Human capital investments and expectations about career and family. *Journal of Political Economy*, 129(5):1361–1424.
- Yum, M. (2022). Parental time investment and intergenerational mobility. International Economic Review.

A Data

A.1 National Longitudinal Study of Adolescent to Adult Health (Add Health)

A.1.1 Description

The National Longitudinal Study of Adolescent to Adult Health (Add Health) survey is a nationally representative longitudinal survey of adolescents in the United States. In the academic year 1994-1995, about 20,000 students in grades 7-12 were sampled to complete an in-home interview. They come from 132 schools, and in 1994-1995, most of them were aged between 12 and 17 years old. In 2016-2018, about 12,300 of them answered the Wave V survey. At the date of the last survey wave, most of the interviewees were aged between 35 and 40 years old. The analysis focuses on the baseline survey in 1994 (Wave I), when interviewees were aged between 12 and 17, and the last follow-up survey in 2018 (Wave V), when interviewees were aged between 35 and 40.

The data set includes detailed information on family background and a rich set of information on neighborhood characteristics. In 1994, we observe the highest education level of the parents of about 17,000 interviewed adolescents, and we have information on residential neighborhood characteristics for about 18,100 adolescents. Information on neighborhoods is available at the census tract level. In addition, Add Health contains questions on the frequency of ten parent-child activities. Add-Health structure allows me to correlate the number of parent-child activities with neighborhood characteristics which can't be done using the more detailed American Time Use Survey (ATUS) (see Appendix Section A.3).

A.1.2 Neighborhood and Parental Time

The Add Health data includes detailed information on parents, children, and neighborhood characteristics, which allows me to construct two parental inputs in the child skill production function: parental time and neighborhood quality. I proxy neighborhood quality by the household median income of the census tract in which the interviewee resided in 1994 and 2018.³³ I create ten synthetic neighborhoods by ranking all census tracts by neighborhood quality and grouping them into ten groups of equal size. One synthetic neighborhood represents a decile of the census tracts distribution in the United States. Thanks to the panel

 $^{^{33}}$ In Appendix Section E.3 I also use the share of residents above 25 with a college degree as a robustness check of the results (Diamond, 2016).

form of the data set, I can observe in which synthetic neighborhood an adolescent lives in 1994-1995 and in which synthetic neighborhood she lives during adulthood, in 2016-2018.

Add Health survey contains information about ten parent-child activities in 1994-1995.³⁴ To proxy for time allocated in childcare, I construct a variable that counts the number of activities that happened over the past four weeks with the mother and the father of the child. I follow the United States Bureau of Labor Statistics (BLS) definition of "primary childcare activities" constructed and exclude two out of the ten events: "shopping", "went to a religious service or church-related event" and.³⁵ The remaining eight activities are: "played a sport", "talked about someone you're dating, or a party you went to", "talked about a personal problem you were having", "worked on a project for school", "talked about other things you're doing in school", "went to a movie, play, museum, concert, or sports event".

A.2 National Historical Geographic Information System (NHGIS)

The National Historical Geographic Information System (NHGIS) provides access to summary tables and time series of population, housing, agriculture, and economic data, along with GIS-compatible boundary files, for years from 1790 through the present and for all levels of U.S. census geography, including states, counties, tracts, and blocks. Data is easily accessible on the IPUMS Website (Manson et al., 2022).

A.3 The American Time Use Survey (ATUS)

A.3.1 Description

The American Time Use Survey (ATUS) is a nationally representative survey of Americans aged 15 or over that provides extensive information on how and where Americans spend their time. From 2003 to 2020, almost 219,000 interviews were conducted, and all of those can be linked to data files from the Current Population Survey (CPS). I use already linked

³⁴The question of interest is: "Which of the things listed on this card have you done with [resident mother/father] in the past four weeks (check all that apply)".

³⁵The definition of "primary childcare activities" that is provided by the United States Bureau of Labor Statistics (BLS) includes time spent providing physical care; playing with children; reading with children; assisting with homework; attending children's events; taking care of children's health needs; and dropping off, picking up, and waiting for children. It does not include activities with children without active childcare, such as "watching television with my child". As a robustness check, I construct an alternative proxy without the activity "went to a movie, play, museum, concert, or sports event".

datasets provided by Hofferth et al. (2020) and available on the IPUMS website. As all the other datasets are from the year 2000, I use the earliest ATUS survey year, 2003.

The ATUS asked interviewees about their activities the day before the interview-the "diary day." For each activity, respondents are asked how long the activity lasted and, for most activities, where they were and who was with them. After completing the time diary, there are additional questions to identify work, volunteering, eldercare, and secondary child-care activities. Several activity categories are then defined by the United States Bureau of Labor Statistics (BLS), among which one is of particular interest for this research project: "primary childcare activities." This activity category includes time spent providing physical care, playing with children; reading with children; assisting with homework; attending children's events; taking care of children's health needs, and dropping off, picking up, and waiting for children. Passive childcare was included as a primary activity (such as "keeping an eye on my son while he swam in the pool"). However, a child's presence during the training is not enough to classify it as childcare; "watching television with my child" is coded as a leisure activity, not as childcare.

A.3.2 Parental Time

To measure parental time, I first restrict the sample to individuals in a two-parent household, defined as married individuals whose youngest child is under age 18. In 2003, 5,597 married parents were interviewed, among which 2,168 have a college degree.³⁶. I use the BLS definition of childcare as "primary childcare activities" and respect the activity coding structure of ATUS to describe how parents from different socioeconomic groups allocate their time between childcare, leisure, and market work. Market work hours include all hours spent in work-related and education-related activities. The rest of the time is considered leisure time. For informational purposes, I divide this last group into two sub-groups: all personal leisure activities and other types of activities.³⁷

³⁶I removed 255 observations that have less than 23 hours of activity a day reported. 92% of the remaining observations have exactly 24 hours of activity a day reported.

³⁷Personal leisure is composed by eight activities: "eat and drink", "personal care", "telephone calls", "professional and personal care services", "religious and spiritual activities", "socializing, relaxing, and leisure", "sports, exercise, and recreation", "volunteer activities". I remove eight hours of sleep needs from "personal care" that includes sleep time, a standard assumption in the literature. Others are "household activities," "household services," "government services and civic obligations," "consumer purchases," "travel," and "caring for and helping non-household and [other] household members." Appendix Table S1 provides detailed information on each of those activities.

		Non- college parents	College parents
Label	Description	Hours	per day
Childcare		1.17	1.58
Caring for and	Time spent in caring for or helping household children	1.17	1.58
helping house-			
hold children			
Work and Education		4.36	4.66
Working and	Time spent in work activities such as working, doing	4.27	4.56
Work-related	activities as part of one's job, engaging in income-		
Activities	generating activities (not as part of one's job), and		
	looking for jobs and interviewing.		
Educational ac-	Time spent in non-work education activities, such as	0.10	0.10
tivities	taking classes, conducting research and homework,		
	administrative tasks, and extracurricular activities		
	except sports.		
Personal leisure		14.39	13.64
Personal care	Time spent in personal care activities such as sleep- ing, grooming, and health-related self care.	9.05	8.66
Eat and drink-	Time spent in activities such as eating and drink-	1.02	1.19
ing	ing not done as work or a volunteer activity, whether		
	the respondent was alone, with others, at home, at a		
	place of purchase, in transit, or somewhere else.		
Socializing,	Time spent in personal interest or leisure activities	3.69	2.88
relaxing, and	such as communicating with others and attending		
leisure	parties and meetings; and leisure activities such as re-		
	laxing, playing (passive) games (unless playing with		
	children only), watching television, playing or listen-		
	ing to music, reading, writing, and all hobbies.		

Table S1: ATUS Activity Coding Structure, 2003

Sports, exercise, and recreation	Time spent in sports, exercise and recreational ac- tivities such as pleasure boating, throwing a Frisbee, kite flying, or ballooning, and active, participatory outdoor games or activities, such as horseshoes, cro- quet, and paintball.	0.25	0.33
Religious and spiritual activi- ties	Time spent in work activities such as working, doing activities as part of one's job, engaging in income- generating activities (not as part of one's job), and looking for jobs and interviewing.	0.14	0.17
Volunteer activ- ities	Time spent in volunteer (unpaid) activities done by the respondent for individuals or institutions through formal organizations, such as unpaid performance arts activities, socializing related to volunteering and attending church service as a volunteer activity.	0.13	0.25
Telephone calls	Time spent in telephone communication activities such as talking on phone, waiting for a phone call or Skyping (2011+).	0.05	0.07
Professional and personal care services	Time spent in activities such as obtaining, receiving, and/or purchasing professional and personal care ser- vices provided by someone else. Professional services include child care, financial, legal, medical and other adult care, real estate, and veterinary. Personal care service activities include massages, haircuts, mani- cures, and tanning at salons.	0.07	0.09
Other		4.04	4.07
Household activities	Time spent in household activities such as maintain- ing their household, household management and or- ganizational activities.	2.13	1.94
Caring for and helping house- hold members (except house- hold children)	Time spent in caring for or helping any adult in the respondent's household, regardless of relation- ship, age, or physical or mental health status.	0.04	0.03

Fotal		24.0	24.0
	bus or train.		
	as commuting, walking someplace or waiting for the		
Travel	Time spent in travel or transportation activities such	1.33	1.51
	internet, at home, or in a store).		
	purchase or rental (in person, via telephone, over the		
chases	of consumer goods, regardless of mode or place of		
Consumer pur-	Time spent in activities such as purchases and rentals	0.43	0.49
	cesses (voting, town hall meetings).		
	in activities that assist or impact government pro-		
	role meetings, court appearances), and participating		
	fulfilling government-required duties (jury duty, pa-		
civic obligations	government-required licenses or paying fines or fees,		
services and	services (police, fire, social services), purchasing		
Government	Time spent in activities such as using government	0.00	0.00
	was the respondent's primary activity.		
	ing, etc.) should be coded here, provided "watching"		
	paid household activities (cooking, cleaning, repair-		
	and construction. Watching someone else perform		
	vices, and vehicle and home repairs, maintenance,		
	ing, cooking, pet care, tailoring and laundering ser-		
	Household services include yard and house clean-		
vices	chasing household services provided by someone else.		
Household ser-	Time spent in activities such as obtaining and pur-	0.01	0.02
members	status.		
non-household	less of relationship, age, or physical or mental health		
and helping	who is not part of the respondent's household, regard-		
Caring for	Time spent in caring for or helping any child or adult	0.10	0.08

Notes: This table provides information on time allocation by married couples with a child below 18 in the household in the United States. Data source: ATUS 2003.

B Equilibrium Computation

The below algorithm uses an iterative method to find the steady state.

1. Make an initial guess for the distribution $F(h, s, m_0, \tilde{\alpha})$ and value function $U(h, s, m_0, \tilde{\alpha})$.

- Given U(h, s, m₀, α̃), compute the policy function τ(h, s, m₀, α̃, m) and the corresponding V(h, s, m₀, α̃, m)
- 3. Make an initial guess for rent prices $\{r_m\}_{m \in \mathbb{M}}$
- 4. Given $V(h, s, m_0, \tilde{\alpha}, m)$, $\tau(h, s, m_0, \tilde{\alpha}, m)$ and $\{r_m\}_{m \in \mathbb{M}}$, compute the share of families $(h, s, m_0, \tilde{\alpha})$ in each neighborhood $(\lambda_m(h, s, m_0, \tilde{\alpha})$ for every m).
- 5. Compute $\{r_m\}_{m \in \mathbb{M}}$ given the share of families in each neighborhood.
- 6. Iterate 3 to 5 until $\{r_m\}_{m \in \mathbb{M}}$ converges.
- 7. Given $\{r_m\}_{m \in \mathbb{M}}$, compute the expected value function $U(h, s, m_0, \tilde{\alpha})$ and based on it, obtain the policy function for time investment $\tau(h, s, m_0, \tilde{\alpha})$.
- 8. Compute the distribution $G(H, T, m_0, h, m)$ given λ_m , and obtain updated subjective beliefs in each neighborhood $\tilde{\alpha}(\tilde{\alpha}, m)$.
- 9. Compute the time invariant distribution $F(h, s, m_0, \tilde{\alpha})$, based on the initial guess, the policy functions for neighborhoods $\lambda_m(h, s, m_0, \tilde{\alpha})$, and $\tau(h, s, m_0, \tilde{\alpha}, m)$, and on beliefs updating $\tilde{\alpha}(\tilde{\alpha}, m)$ obtained above.
- 10. Iterate from 1 to 9 until $F(h, s, m_0, \tilde{\alpha})$ converges.

C Theory Appendix

C.1 Modeling a micro-foundation of the selection neglect bias

The strength of the bias π can be micro-founded following Jehiel (2018) who develops a theoretical framework of selection neglect with bounded signals. Assume young agents receive informative but noisy and bounded signals about their adult neighbors' abilities.³⁸ The signal noisiness could capture the fact that there is no real way to perfectly gauge ability—which can be interpreted as a combination of intelligence and luck—by simply observing people. The signal boundedness would embed the tendency to classify people's abilities within predefined categories.³⁹ Intelligence tests always have a scale with a predefined minimum and

 $^{^{38}}$ Jehiel (2018) develops a theoretical framework of entrepreneurial decisions with bounded signals about the quality of businesses and selection based on success. He obtains over-optimism among entrepreneurs in equilibrium.

³⁹The signal can be thought of as continuous or discrete. For computational reasons, in practice, every shock is discretized.

maximum level. The IQ test, for instance, classifies people's Intelligence Quotient between "very superior" and "extremely low." Note that the bounds of the signals are the same across neighborhoods. This common scale assumption could be motivated by identical reference points regarding abilities. In every neighborhood, young agents interact with other young agents who are representative of the population with respect to abilities. They can all watch national media and gauge the speaker's ability. In a given neighborhood m, young agents' perception of the average local ability among adults would then be defined by:

$$\overline{\tilde{a}}_m = \int_{-\infty}^{+\infty} \int_{-d}^{d} \tilde{a} f(\tilde{a}|a) l(a|m) d\tilde{a} da,$$

while the actual average local ability is:

$$\overline{a}_m = \int_{-\infty}^{+\infty} a \ l(a|m) \ da,$$

where conditional on the shock realization a, the signal realization \tilde{a} is distributed according to the density $f(\cdot|a) = \mathcal{N}(a, \sigma_s)$ with full support in [-d, d] with z, the bound, a real value. The precision of the signal is governed by the signal variance σ_s^{2} . The distribution of adults' ability in a given neighborhood m is denoted by $l(\cdot|m)$ and results from residential decisions in equilibrium. Note that, because of the bounds, despite the informativeness of the signal, the expected perceived ability is not always equal to the ability. The signal is upward biased whenever the actual ability is below the average ability in the economy ($\forall a \leq 0$ then $\mathrm{E}\left[\tilde{a}|a\right] \geq a$), and downward biased whenever the actual ability is above the average ability in the economy ($\forall a \geq 0$ then $\mathrm{E}\left[\tilde{a}|a\right] \leq a$). Intuitively, because the conditional signal is bounded, if the realization is closer to one of the bounds, many more high signals will be censored by this bound than by the other.⁴⁰ Consequently, in neighborhoods in which the average local ability is below the average ability in the economy, young agents overestimate average local ability (if $\overline{a}_m \leq 0$ then $\overline{a}_m \geq \overline{a}_m$), and conversely if the average local ability is above the average ability in the economy (if $\overline{a}_m \geq 0$ then $\overline{a}_m \leq \overline{a}_m$).

In the limit, if the signal variance (σ_s) tends to zero, or if the bounds (d) tend to infinity, agents' perception about their neighbors' ability shocks would always be equal to the truth and $\overline{\tilde{a}}_m = \overline{a}_m$. Note that at any given level of bounds below infinity, the signal variance σ_s^2 governs the precision of the perceived local ability and regulates the strength of the bias in the estimation, which allows a direct mapping with π .

⁴⁰See Appendix Figure S1 for an illustration.

C.2 Proofs

Assume $x \sim \mathcal{N}(\overline{\mu}, \sigma_s^2)$ and define the function $\operatorname{bound}(x, d) := x \mathbbm{1}_{\{-d \le x \le d\}} + d\mathbbm{1}_{\{x > d\}} - d\mathbbm{1}_{\{x < d\}}$.

Let d > 0 constant and y := bound(x, d). Let Φ the CDF of the standard normal distribution and ϕ the PDF of the standard normal distribution.

Then it holds:

- 1. If $\overline{\mu} \ge 0$ then $\mathbb{E}(y) \ge 0$ and if $\overline{\mu} \le 0$ then $\mathbb{E}(y) \le 0$
- 2. If $\overline{\mu} \ge 0$ then $\mathbb{E}(y) \le \overline{\mu}$ and if $\overline{\mu} \le 0$ then $\mathbb{E}(y) \ge \overline{\mu}$
- 3. $\lim_{\sigma_s \to 0} \mathbb{E}(y) = \overline{\mu}$ and $\lim_{d \to +\infty} \mathbb{E}(y) = \overline{\mu}$
- 4. $\lim_{\sigma_s \to +\infty} \mathbb{E}(y) = 0$

Figure S1 illustrates a conditional signal distribution of y given $d > \overline{\mu} > 0$.

Preliminary common results for (1)-(4): Assume $\overline{\mu} \ge 0$

(a) Let

$$\mathbb{E}(y) = \int_{-d}^{d} \frac{u}{\sigma_s} \phi\left(\frac{u-\overline{\mu}}{\sigma_s}\right) \, du + d \, \left(1 - \Phi\left(\frac{d-\overline{\mu}}{\sigma_s}\right)\right) - d \, \Phi\left(\frac{-d-\overline{\mu}}{\sigma_s}\right)$$

- (b) Let $u = v + \overline{\mu}$. By properties of the Gaussian distribution, $\forall u \ge 0 \ \phi(v) = \phi(-v)$ and $\phi(v) \ge \phi(-v 2\overline{\mu})$ or $\phi(u \overline{\mu}) = \phi(-u + \overline{\mu})$ and $\phi(u \overline{\mu}) \ge \phi(-u \overline{\mu})$
- (c) Let

$$\mathbb{E}(x) = \int_{-\infty}^{\infty} \frac{u}{\sigma_s} \phi\left(\frac{u-\overline{\mu}}{\sigma_s}\right) du$$

= $\int_{-d}^{d+2\overline{\mu}} \frac{u}{\sigma_s} \phi\left(\frac{u-\overline{\mu}}{\sigma_s}\right) du + (d+2\overline{\mu}) \left(1 - \Phi\left(\frac{d+\overline{\mu}}{\sigma_s}\right)\right) - d\Phi\left(\frac{-d-\overline{\mu}}{\sigma_s}\right)$
= $\overline{\mu}$

Proof. (1) Assume $\overline{\mu} \ge 0$. By (b),

$$\int_{0}^{d} \frac{1}{\sigma_{s}} u \phi\left(\frac{u-\overline{x}}{\sigma_{s}}\right) du \geq \left| \int_{0}^{d} \frac{1}{\sigma_{s}} \left(-u\right) \phi\left(\frac{-u-\overline{x}}{\sigma_{s}}\right) du \right| = \left| \int_{-d}^{0} \frac{1}{\sigma_{s}} u \phi\left(\frac{u-\overline{x}}{\sigma_{s}}\right) du \right|$$

and

$$\left(1 - \Phi\left(\frac{d - \overline{x}}{\sigma_s}\right)\right) \ge \Phi\left(\frac{-d - \overline{x}}{\sigma_s}\right) \ge 0$$

Hence, by (a), $\mathbb{E}(y) \ge 0$.

By the symmetry of the Gaussian distribution, if $\overline{\mu} \leq 0 \implies \mathbb{E}(y) \leq 0$.

(2) Assume $\overline{\mu} \ge 0$. By (c),

$$\begin{split} \overline{\mu} &= \int_{-d}^{d} \frac{u}{\sigma_{s}} \phi\left(\frac{u-\overline{\mu}}{\sigma_{s}}\right) \, du \, + \, \int_{d}^{d+2\overline{\mu}} \frac{u}{\sigma_{s}} \phi\left(\frac{u-\overline{\mu}}{\sigma_{s}}\right) \, du \\ &- \, d \, \Phi\left(\frac{-d-\overline{\mu}}{\sigma_{s}}\right) \, + \, (d+2\overline{\mu}) \, \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right) \\ &\geq \int_{-d}^{d} \frac{u}{\sigma_{s}} \phi\left(\frac{u-\overline{\mu}}{\sigma_{s}}\right) \, du \, + \, d \, \left(1-\Phi\left(\frac{d-\overline{\mu}}{\sigma_{s}}\right) - \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right)\right) \\ &- \, d \, \Phi\left(\frac{-d-\overline{\mu}}{\sigma_{s}}\right) \, + \, (d+2\overline{\mu}) \, \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right) \\ &= \int_{-d}^{d} \frac{u}{\sigma_{s}} \phi\left(\frac{u-\overline{\mu}}{\sigma_{s}}\right) \, du \, + \, d \, \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right) \\ &- \, d \, \Phi\left(\frac{-d-\overline{\mu}}{\sigma_{s}}\right) \, + \, 2\overline{\mu} \, \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right) \\ &= \mathbb{E}(y) \, + \, 2\overline{\mu} \, \left(1-\Phi\left(\frac{d+\overline{\mu}}{\sigma_{s}}\right)\right) \quad (\text{by (a)}) \\ &\geq \mathbb{E}(y) \end{split}$$

Hence, $\mathbb{E}(y) \leq \overline{\mu}$.

By the symmetry of the Gaussian distribution, if $\overline{\mu} \leq 0 \implies \mathbb{E}(y) \geq \overline{\mu}$.

(3) Note $\lim_{x\to+\infty} \Phi(x) = 1$ and $\lim_{x\to+\infty} \Phi(-x) = 0$. By (a)

$$\lim_{d \to +\infty} \mathbb{E}(y) = \overline{\mu}$$

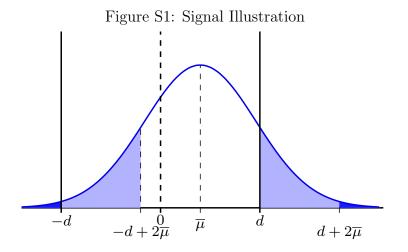
Trivially,

$$\lim_{\sigma_s \to 0} \mathbb{E}(y) = \overline{\mu}$$

(4) Note $\lim_{\sigma_s \to +\infty} \int_{-d}^{d} \frac{u}{\sigma_s} \phi\left(\frac{u-\overline{\mu}}{\sigma_s}\right) du = 0$ and $\lim_{\sigma_s \to +\infty} \Phi\left(\frac{d-\overline{\mu}}{\sigma_s}\right) = 0.5.$

By (a)

$$\lim_{\sigma_s \to +\infty} \mathbb{E}(y) = 0$$



Notes: This Figure illustrates a conditional signal distribution of y given $d > \overline{\mu} > 0$.

D Additional Information on the Calibration

D.1 Parental Time

Table S2 summarizes parents' time use in the United States by education. I first restrict the sample to individuals in a two-parent household, defined as married individuals whose youngest child is under age 18.⁴¹ In 2003, 5,597 married parents were interviewed, among which 2,168 have a college degree.^{42,43} As standard in the literature, I assume 16 hours of disposable hours and eight hours of sleep needs per day.

Both parental time and market work time increase in education. Parents with a college degree spend about 1.6 hours per day in childcare activities and 4.7 hours in market work

 $^{^{41}}$ I only keep two-parent households for consistency with the model that does not consider marital status. 78% of parents in the sample are married.

 $^{^{42}}$ Parent's education is defined as the highest level of education of the respondent. Using the highest education level of both parents or of the mother doesn't change the results in Table S2.

⁴³As, for Table S1, I removed 255 observations that have less than 23 hours of activity a day reported. 92% of the remaining observations have exactly 24 hours of activity a day reported.

activities, while parents without a college degree spend 1.2 hours in childcare and 4.4 hours in market work.⁴⁴ Leisure time mechanically decreases in education. It is interesting to note, however, that this decrease is entirely driven by college parents spending less time on personal leisure activities compared to non-college parents. Time spent in other types of activities is relatively constant across educational groups.⁴⁵ In the following, I consider an endowment of 16 disposable hours per day and normalize it to one. Parental time patterns are moments to match.

	Non-college graduated parents		College graduated parents	
	Hours per day	% of total	Hours per day	% of total
Market work	4.4	27.5%	4.7	29.4%
Childcare	1.2	7.5%	1.6	10.0%
Leisure				
Personal leisure	6.4	40.0%	5.6	35.0%
Other	4.0	25.0%	4.1	25.6%
Total	16.0	100%	16.0	100%

Table S2: Parents' Time Allocation by Education, ATUS 2003

Notes: This table provides information on time allocation by married parents in the United States. The data source is ATUS 2003. Childcare activity follows the BLS definition of "primary childcare activities." Market work contains all work-related and educational activities. Leisure includes all the other activities. For more details on activity grouping, see Appendix Table S1.

D.2 Synthetic Neighborhoods Characteristics

Table S3 summarizes the characteristics of these neighborhoods. By construction, median household income increases with neighborhood quality. As expected, so does the fraction of individuals above 25 with a college degree (Column (2)).⁴⁶ Note that housing expenditure shares decrease with neighborhood quality (Column (4)) which suggests and motivates non-homothetic preferences.

 $^{^{44}}$ The number of children is close to two for both groups. Time per child in a two-parent household is very similar to childcare time, 1.1 hours for non-college and 1.6 hours for college-graduated households.

⁴⁵Appendix Table S1 describes how parents allocate their time spent in each of the ATUS activities.

 $^{^{46}}$ See Appendix Section A.2 for more details information on each of the variables used to calibrate the model.

	Median household income (USD)	Fraction of people aged 25+ with college	Fraction below poverty level	Median rent over median household	Fraction of households
	(1)	degree (2)	(3)	income (4)	(5)
Neighborhood D1	20,638	0.113	0.358	0.286	0.071
Neighborhood D2	$28,\!883$	0.134	0.233	0.234	0.088
Neighborhood D3	$34,\!259$	0.158	0.167	0.211	0.093
Neighborhood D4	$38,\!652$	0.187	0.133	0.197	0.096
Neighborhood D5	42,957	0.212	0.105	0.187	0.100
Neighborhood D6	47,552	0.236	0.085	0.177	0.105
Neighborhood D7	$52,\!547$	0.268	0.069	0.170	0.107
Neighborhood D8	$58,\!810$	0.311	0.054	0.163	0.111
Neighborhood D9	67,780	0.386	0.042	0.156	0.114
Neighborhood D10	91,273	0.528	0.030	0.141	0.115

Table S3: Characteristics of Synthetic Neighborhoods

Notes: This table provides average sociodemographic characteristics in the ten synthetic neighborhoods. The data source is the NHGIS data from 2000 at the census tract level for the 100 biggest commuting zones. The associated distributions serve as targeted and untargeted moments for the model calibration.

D.3 Estimated Parameters: Neighborhood Choices and College Graduation

For two primary purposes, I use the AddHealth survey, detailed in Appendix Section A.1. First, to compute intergenerational residential mobility. To do so, as in the NHGIS data analysis, I create ten synthetic neighborhoods in 1994-1995, 2008-2009, and 2016-2018 by ranking all census tracts by median household income and grouping them into ten groups of equal size. Thanks to the panel form of the data set, I can observe in which synthetic neighborhood an adolescent lived in 1994-1995 and in which artificial neighborhood she lived during adulthood, in 2008-2009 and 2016-2018. I restrict the sample to people no longer living at their parent's place. Even though, due to attrition, samples are smaller in Wave V than in Wave IV, I use estimates from Wave V.⁴⁷ In 2016-2018, interviewees were older, between 35 and 40, and more likely to be married than ten years before.⁴⁸ 30.2% of adolescents who lived in a first decile census tract in 1994 lived in the same decile census tract in 2016-2018. In the sixth decile, this percentage falls to 13.0%.

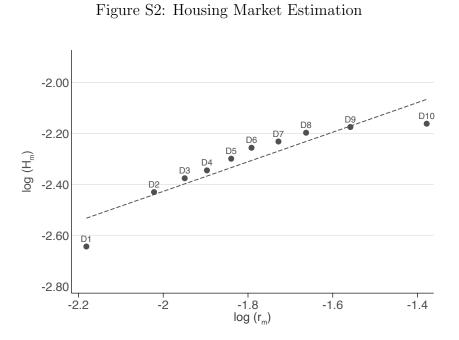
⁴⁷All observations are weighted by the sampling weights of the corresponding wave provided by AddHealth. When variables from different waves are used simultaneously, the weights I use are from the latest wave.

⁴⁸Intergenerational residential mobility patterns are similar whether I use Wave V or Wave IV.

Second, I use AddHealth to estimate the individual probability of having a college degree conditional on parents and child variables. In the sample, anyone with at least a bachelor's degree is considered to have a college degree. Here again, because interviewees are older and more likely to have completed their education in 2016-2018 than in 2008-2009, I use data from Wave V to estimate the highest level of education. To proxy for children's realized human capital, I use an average of Wave II (1996) grades in English, mathematics, social science, and science. Information on parents' highest education level and income comes from the parent survey conducted in 1994-1995.

T <u>able S4: Esti</u>	mated 1	<u>Paramet</u> ers
	Colleg	ge
	gradu	ation
	proba	bility
γ_1	-3.83	(0.35)
γ_2	0.35	(0.02)
γ_3	0.15	(0.02)
γ_4	1.11	(0.11)
Pseudo R^2	0.28	

Notes: The table shows the weighted logit regression results. The regression includes county fixed effects. Robust standard errors are in parenthesis. These are all the estimated parameters.



Notes: This Figure displays the estimated housing supply equation, as a function of the relative rent price. Data points show actual rent prices and density for each of the ten synthetic neighborhoods.

D.4 Moments

Intergenerational residential mobility:

Data: I use the Add Health survey that contains census tract level information. The sample is restricted to interviewees who do not live in their parent's houses in adulthood. Census tracts are ordered by household median income and divided into ten synthetic neighborhoods. For each decile neighborhood, I compute the share of children who, in adulthood, choose to live in the same decile of the neighborhood quality distribution as their parents.

Model: For each neighborhood, I compute the share of children who, in adulthood, choose to live in the same decile of the neighborhood quality distribution as their parents.

Other moments:

Table S5	: Moments	Description
----------	-----------	-------------

Moment	Description	Data restriction	Source
Earnings			
Share college	Fraction of college parents in the first quartile	100 biggest commuting zones - fami-	ACS 2000
parents in Q1	of the income distribution over the fraction of	lies with a own child below 18	
over Q4	college parents in the fourth quartile of the		
	income distribution.		
Earnings ratio	Household income of non-college parents over	100 biggest commuting zones - fami-	ACS 2000
non-college -	household income of college parents.	lies with a own child below 18	
college			
Income Gini [in-	Families' income Gini, transformed in a 20	100 biggest commuting zones - fami-	ACS 2000
equality]	years Gini using the 2002 Shorrocks mobiliy	lies with a own child below 18	
	index estimated by Kopczuk et al. (2010).		

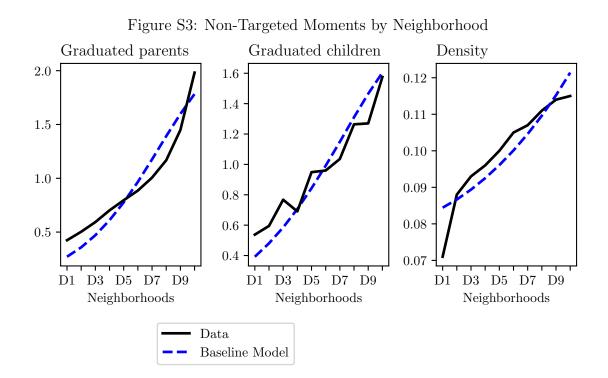
Residential mobility

Census tract	Gini coefficient across the ten synthetic neigh-	100 biggest commuting zones - fami-	NHGIS
Gini [segrega-	borhoods household median income.	lies with a own child below 18	2000
tion]			
Neighborhood	For families with below-median income (p =	Tax records covering the U.S. pop-	Chetty and
effect (25th	25). Simulate moves to every neighborhoods.	ulation, spanning 1996-2012. 100	Hendren
pct.)	Regress children's income on fixed effects for	biggest commuting zones (CZ).	(2018a)
	each neighborhood controlling for origin-by-	Within CZ estimates. The authors	
	destination fixed effects.	use income ranks at age 26 because	
		of outliers. In addition, they control	
		for the fraction of childhood spent in	
		a county.	
Neighborhood	For families with above-median income (p =	Tax records covering the U.S. pop-	Chetty and
effect (75th	75). Simulate moves to every neighborhoods.	ulation, spanning 1996-2012. 100	Hendren
pct.)	Regress children's income on fixed effects for	biggest commuting zones (CZ).	(2018a)
	each neighborhood controlling for origin-by-	Within CZ estimates. The authors	
	destination fixed effects.	use income ranks at age 26 because	
		of outliers. In addition, they control	
		for the fraction of childhood spent in	
		a county.	
Residential im-	Fraction of children born in the first synthetic	1994-2018. Interviewees who do not	AddHealth
mobility $(D1)$	neighborhood who live in this same neighbor-	live in their parent's houses in adult-	Wave I and
	hood when they are adults.	hood (2018).	Wave V
Social mobility			

Social mobility

Rank-rank coef-	Regression coefficient of child household in-	Tax records covering the U.S. popu-	Chetty
ficient	come rank on parental househod income rank.	lation, spanning 1996-2012.	et al.
			(2014)
Parental time			
Parental time	Income regression coefficient of parental time	Two-parent households with a own	ATUS 2003
income coeff.	on income quartile and college graduation sta-	child below 18. Weighted. Addi-	
	tus of the parents.	tional controls on gender, child age,	
		number of children, and date of in-	
		terview.	
Parental time	Income regression coefficient of parental time	Two-parent households with a own	ATUS 2003
education coeff.	on income quartile and college graduation sta-	child below 18. Weighted. Addi-	
	tus of the parents.	tional controls on gender, child age,	
		number of children, and date of in-	
		terview.	
Parental time	Average parental time of non-college parents.	Two-parent households with a own	ATUS 2003
non-college		child below 18. Weighted.	
parents			

D.5 Model Fit for Additional Non-Targeted Moments



Notes: This Figure shows two non-targeted moments across neighborhoods: the share of graduated parents and the share of graduated children. The third panel presents the population density by neighborhood which is matched by estimating the housing supply function parameters. The solid line shows the data moments, and the dashed line shows the model-simulated analogs. Data Source: NHGIS.

D.6 Perfect Information Model

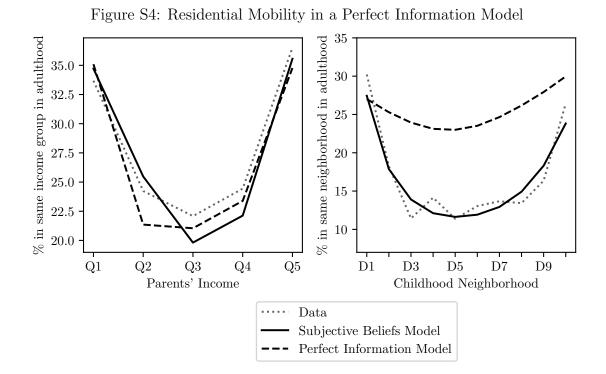
This section describes the calibration of a model with perfect information ($\pi = 0$). Parents' preferences take the following forms:

$$\log\left(c\right) + \frac{\left(1 - \overline{\ell_s} - \kappa \tau\right)^{1 - \frac{1}{\psi}}}{1 - \frac{1}{\psi}} + \iota \mathbb{1}_{m_0 = m} + \nu \varepsilon_m + b \mathbb{E}\left[\mathcal{V}\left(h', s', m, \alpha\right)\right]$$

Parameter	Description	Moment	Data	Model			
Preferences	Preferences and Labor Market						
b = 0.65	Altruism	Ratio share college parents Q1 to Q4	0.102	0.118			
$\kappa = 0.7$	Parental time disutility	Parental time non-college parents	0.075	0.079			
$\iota = 0.012$	Place of birth preference	Residential mobility (D1)	0.295	0.270			
$\omega~=~0.01$	College wage premium	Earnings ratio non-college - college	0.554	0.558			
Neighborho	oods						
$\sigma_m = 0.16$	Neighborhood quality	Neighborhood effect (25th pct.)	0.062	0.065			
$\nu = 0.02$	Taste shock variance	Census tract Gini	0.231	0.198			
Skill Forma	ation: $h' = \left(\left(\gamma \left(\frac{\tau}{\overline{\tau}} \right)^{\varphi} + (1 - \gamma) \right)^{\varphi} \right)$	$(-\gamma) m^{\varphi} \Big)^{\frac{1}{\varphi}} + \underline{i} \Big)^{\alpha} h^{1-\alpha} \exp(a')$ with a'	$\prime \sim \mathcal{N}(0)$	$,\sigma_a)$			
$\alpha = 0.72$	Elasticity of investments	Rank-rank coefficient	0.341	0.344			
$\gamma = 0.45$	Parental time share	Neighborhood effect (75th pct.)	0.046	0.057			
φ = -5	$\operatorname{Substitutability}$	Income gradient in parental time	0.140	0.114			
$\sigma_a = 0.55$	Ability shock variance	Income Gini	0.336	0.329			
Heterogene	Heterogeneous Parental Behavior						
		Education parental time gap	0.750	0.926			
		Neighborhood quality correlation	0.417	0.276			

Table S6: Internally Calibrated Parameters Assuming Perfect Information

Notes: This table reports the internally calibrated parameters assuming perfect information ($\pi = 0$) and the observed and simulated moments associated with the parameter estimates.



Notes: Left panel shows the share of children who, when they are adults, are in the same household income quintile as their parents. Right panel shows the share of children who still live in their childhood neighborhood quality when they are adults. Data moments are in dotted-line, subjective beliefs model simulated analogs in solid-line, and perfect information model in dashed-line.

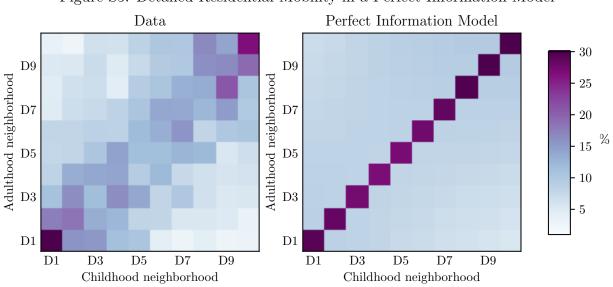


Figure S5: Detailed Residential Mobility in a Perfect Information Model

Notes: This Figure shows residential mobility between childhood and adulthood in the data (left panel), and their perfect information model simulates analogs (right panel). The x-axis contains the ten synthetic childhood neighborhoods, and the y-axis is the ten synthetic adulthood neighborhoods. The frequency of moves is represented by cell colors, with larger values in darker squares.

D.7 Perfect Information Model with Heterogeneity

This section describes the calibration of a model with perfect information but with heterogeneous preferences. Parents' preferences feature an heterogeneous altruism parameter by education and I assume a quadratic moving cost function. Parents' preferences take the following forms:

$$\log(c) + \frac{(1 - \overline{\ell_s} - \kappa \tau)}{1 - \frac{1}{\psi}}^{1 - \frac{1}{\psi}} + \iota \mathbb{1}_{m_0 = m} - \xi(m_0 - m)^2 + \nu \varepsilon_m + b_s \mathbb{E}\left[\mathcal{V}(h', s', m, \alpha)\right]$$

Table S7 and Figure 1 suggest that additional heterogeneity is needed in order to match non-targeted moments. Parents' preferences need to feature an heterogeneous altruism parameter by education, a quadratic moving cost function, and heterogeneous preference for childhood neighborhood ι_{m_0} . Figure S6 shows the fit of the alternative model with additional heterogeneity in preference for childhood neighborhood. In particular, the preference parameter for the worse neighborhood is $\iota_1 = 0.0035$, while in the best neighborhood it is

Parameter	Description	Moment	Data	Model				
Preferences and Labor Market								
$b_0 = 0.6$	Non college altruism	Ratio share college parents $Q1$ to $Q4$	0.102	0.115				
$\kappa = 0.55$	Parental time disutility	Parental time non-college parents	0.075	0.074				
$\iota = 0.0035$	Place of birth preference	Residential mobility (D1)	0.302	0.272				
$\omega = 0.0001$	College wage premium	Earnings ratio non-college - college	0.554	0.558				
Neighborhoods								
$\sigma_m = 0.16$	Neighborhood quality	Neighborhood effect (25th pct.)	0.062	0.061				
ν = 0.01	Taste shock variance	Census tract Gini	0.231	0.190				
Skill Formation: $h' = \left(\left(\gamma \left(\frac{\tau}{\overline{\tau}} \right)^{\varphi} + (1 - \gamma) m^{\varphi} \right)^{\frac{1}{\varphi}} + \underline{i} \right)^{\alpha} h^{1-\alpha} \exp(a')$ with $a' \sim \mathcal{N}(0, \sigma_a)$								
$\alpha = 0.7$	Elasticity of investments	Rank-rank coefficient	0.341	0.358				
$\gamma = 0.45$	Parental time share	Neighborhood effect (75th pct.)	0.046	0.056				
φ = -5.0	Substitutability	Income gradient in parental time	0.140	0.106				
$\sigma_a = 0.55$	Ability shock variance	Income Gini	0.336	0.329				
Heterogeneous Parental Behavior								
$b_1 = 0.7$	College altruism	Education parental time gap	0.750	0.868				
$\xi = 0.0003$	Quadratic moving costs	Neighborhood quality correlation	0.417	0.458				

Table S7: Internally Calibrated Parameters - Alternative Model with Perfect Information

Notes: This table reports the internally calibrated parameters of the extended alternative model with perfect information and the observed and simulated moments associated with the parameter estimates.

three times lower with $\iota_{10} = 0.0012$ and in middle-quality neighborhood thirty times lower with $\iota_5 = 0.0001$.

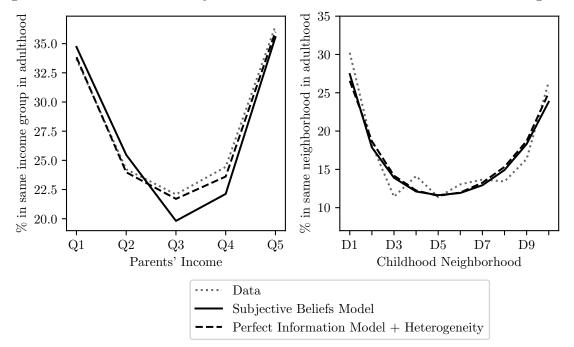


Figure S6: Residential Mobility in Alternative Model with A@dditional Heterogeneity

Notes: The left panel shows the share of children who, when they are adults, are in the same household income quintile as their parents. The right panel shows the share of children who still live in their childhood neighborhood quality when they are adults. Data moments are in dotted-line, subjective beliefs model simulated analogs in solid-line, and perfect information model with highly heterogeneous preferences in dashed-line.

E Neighborhood Quality and Parental Time in the United States

In addition to the extensive subjective beliefs literature, the model builds on suggestive evidence from the National Longitudinal Study of Adolescent to Adult Health (Add Health). In this section I derive and test for two implications of the model. None of the implications are rejected which comforts the plausibility of the social learning mechanism.

E.1 Correlation between Time and Neighborhood

Suppose neighborhood quality and parental time are two inputs of the technology of skill formation. Assume parents' decisions are driven by their perceived value of the returns to both inputs – neighborhood quality and parental time. All else equal, parents with low (high) subjective beliefs will tend to live in worse (better) quality neighborhoods and spend less (more) time with their children. I expect to see a positive correlation between time and neighborhood quality in the data due to the omitted subjective beliefs variable. The data support this assumption.

The Add Health data includes detailed information on parents, children, and neighborhood characteristics, which allows me to construct two parental inputs in the child skill production function: parental time and neighborhood quality. Appendix Section D.3 describes the variable construction. As a first step, I verify the two constructed variables correctly proxy for two parental inputs of the technology of skill formation. Columns (1) and (2) of Table S8 show that parental time and neighborhood quality positively correlate with later child skills. Conditional on other parents' socioeconomic status (SES), the number of parent-child activities and neighborhood quality co-move with the graduation probability measured twenty-two years later. All coefficients are positive and significant at a one percent level. Motivated by this evidence, in the following, I consider the parental time and neighborhood quality variables are good proxies for parental inputs of the technology of skill formation.⁴⁹

Columns (3) and (4) of Table S8 display a positive and significant correlation between parental time measured by the number of parent-child activities done over four weeks and standardized neighborhood quality proxied by household median income.⁵⁰ Note that in both regressions of Column (3) and (4) of Table S8, I control for school ID fixed effects. A systematic difference in school characteristics is not what drives the correlation. Nevertheless, research finds that parental time increases with parents' education in the United States (see Doepke et al. (2022) for a review).⁵¹ This observed correlation could be driven by a neighborhood composition effect. In Column (4) of Table S8, I control for three variables measuring households' socioeconomic status: parents' highest level of education, family income, and parent's marital status.⁵² The sample size shrinks to 12,633 observations due to

⁴⁹Appendix Table S9 presents the OLS regression coefficients with a different definition of neighborhood quality and parental time variables. Results are robust to definition changes.

⁵⁰The results are robust to the use of alternative proxies for parental inputs. See Appendix Table S9.

⁵¹In Appendix D.1 I analyze the ATUS data set, and consistent with Guryan et al. (2008), I find a positive relationship between parental time and parental education.

⁵²Not displayed in the table, the coefficient of parents' education is positive and significant, which is

missing values in household characteristics variables, but the relationship remains positive and significant at a one percent level. This suggests that neighborhood composition effect does not drive all the correlation between the two parental inputs.

	College Graduation 2016-2018		Parental Time 1994-1995		Neighborhood (std) 2016-2018	
	(1)	(2)	(3)	(4)	(5)	(6)
Neighborhood (std)	0.56***		0.212***	0.078***	0.146***	0.111**
1994-1995	(0.012)		(0.03)	(0.028)	(0.038)	(0.043)
Parental Time	. ,	0.031^{***}	. ,	. ,	. ,	. ,
1994-1995		(0.006)				
Race		× ,				0.08
						(0.051)
Controls:						
Childhood SES	yes	yes	no	yes	yes	yes
Adulthood SES	no	no	no	no	no	yes
Same decile census tract	no	no	no	no	yes	yes
School ID FE	yes	yes	yes	yes	no	no
Commuting zone FE	no	no	no	no	yes	yes
No. of obs.	8,518	$8,\!543$	17,102	$12,\!633$	7,982	6,064
Clusters	101	101	120	105	97	90

Table S8: Parental Time and Neighborhood Quality, Add-Health 1994-1995 and 2016-2018

Notes: This table provides between parental investment choices and college graduation (Columns (1) and (2)) correlations between parental investment choices (Columns (2) and (3)) and between childhood and adulthood neighborhood quality (Columns (5) and (6)). Socioeconomic status variables are family income, highest education level, and marital status. See Appendix Section A.1 for details on variable construction. The dependent variables are indicated in the column title. All regressions control for age fixed effects. All observations are weighted by Wave specific sample weights provided by AddHealth. Standard errors displayed in brackets are clustered at the county level. *p<0.1; **p<0.05; ***p<0.01.

While this result is consistent with the assumption of parental beliefs being an omitted variable, it is also compatible with a human capital production function in which neighborhood quality and parental time are complementary inputs. There is no consensus in the literature about this relationship.⁵³

consistent with the educational gradient in childcare time observed in ATUS.

⁵³Chyn and Daruich (2022) find a complementarity between time and neighborhoods, but Agostinelli (2018) and Agostinelli et al. (2022)'s calibrated models imply that parental time and environment quality are substitute inputs in producing children's skills. To my knowledge, all empirical estimates of the relationship between parental time and environment quality suggest that they are substitutes (Kling et al., 2001; Pop-Eleches and Urquiola, 2013; Das et al., 2013; Kiessling, 2021).

E.2 Childhood Neighborhood and Adulthood Choices

The second testable implication of the mechanism is that childhood neighborhood quality and later parental decisions, including neighborhood quality, are positively correlated due to social learning. In poor (wealthy) neighborhoods, I expect children to become pessimistic (over-optimistic) about parenting and later on to under-(over-)invest in their own child's human capital. In the data, childhood neighborhood quality should be positively correlated with later neighborhood choices.

Column (5) of Table S8 displays a positive and significant correlation between childhood (Wave I) and adulthood (Wave V) neighborhood quality. I restrict the sample to interviewees who do not live with their parents and control for commuting zone and age fixed effects. The correlation remains highly significant even after controlling for household income, marital status, and education status. Other factors might affect residential choices. Racial discrimination and wealth are two of them. In Column (6) of Table S8, to proxy for inherited wealth, I control for three variables measuring the parents' socioeconomic status: parents' highest level of education, family income, and parents' marital status. In addition, I control for the race of the interviewee.⁵⁴ The coefficient of relationships between neighborhood qualities barely decreases and remains highly significant. Interestingly, the race coefficient is insignificant, suggesting that race is not the main driver of residential quality choices after controlling for neighborhood quality.⁵⁵

Neither of the two testable implications of the model is rejected. Combined with the extensive literature on subjective beliefs and the great fit of the calibrated model, this suggestive evidence supports the plausibility of the social learning mechanism.

 $^{^{54}\}mathrm{The}$ variable is one if the race is white, zero otherwise.

⁵⁵The results are robust to the use of the fraction of adults with a college degree for neighborhood quality. See Appendix Table S9.

E.3 Robustness checks

	College Graduation 2016-2018		Parental Time 1994-1995		Neighborhood 2016-2018	
	(1)	(2)	(3)	(4)	(5)	(6)
Neighborhood	0.448***		0.758***	0.451***	0.25***	0.211***
1994-1995	(0.1)		(0.195)	(0.185)	(0.037)	(0.032)
Parental Time		0.029***				
1994-1995		(0.007)				
Race						-0.003
						(0.008)
Controls:						
Childhood SES	yes	yes	no	yes	yes	yes
Adulthood SES	no	no	no	no	no	yes
Same decile census tract	no	no	no	no	yes	yes
School ID FE	yes	yes	yes	yes	no	no
Commuting zone FE	no	no	no	no	yes	yes
No. of obs.	8,525	8,543	17,073	12,608	7,952	6,039
Clusters	101	101	120	105	97	90

Table S9: Parental Time and Neighborhood Quality, Add-Health 1994-1995 and 2016-2018

Notes: This table provides between parental investment choices and college graduation (Columns (1) and (2)) correlations between parental investment choices (Columns (2) and (3)) and between childhood and adulthood neighborhood quality (Columns (5) and (6)). Socioeconomic status variables are family income, highest education level, and marital status. See Appendix Section A.1 for details on variable construction. The dependent variables are indicated in the column title. All regressions control for age fixed effects. All observations are weighted by Wave specific sample weights provided by AddHealth. Standard errors displayed in brackets are clustered at the county level. *p<0.1; **p<0.05; ***p<0.01.